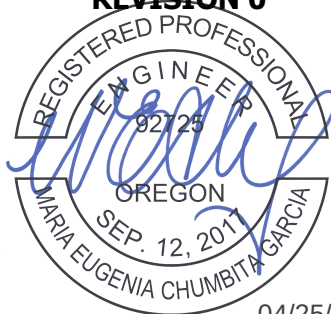


**Reed College Central Plant Upgrade
CALCULATIONS
SUBMITTAL**

REVISION 0



April 23, 2025 04/25/2025
Renews: 12/31/2025

CoreBrace Project #6903



www.CoreBrace.com

APPROVED ☒ REVISE & RESUBMIT ☐
REJECTED ☐ APPROVED AS CORRECTED ☐

APPROVAL IS ONLY FOR GENERAL COMPLIANCE WITH THE CONTRACT DOCUMENTS AND DESIGN CONCEPT OF THE PROJECT. ANY ACTION SHOWN IS SUBJECT TO THE REQUIREMENTS OF THE PLANS AND SPECIFICATIONS. THE CONTRACTOR IS RESPONSIBLE FOR: CONFIRMING AND CORRELATING DIMENSIONS, FABRICATION AND CONSTRUCTION TECHNIQUES, COORDINATION OF THEIR WORK WITH OTHER TRADES, AND THE SATISFACTORY PERFORMANCE OF THEIR WORK.

JAMES G. PIERSON, INC.
CONSULTING STRUCTURAL ENGINEERS
PORTLAND, OREGON

BY: Peter Pierson DATE: 04/29/2025

Reed College Central Plant Upgrade

Calculation Submittal Package

Description

Section 1 Strain, β , and ω Determination and Summary Tables

Section 2 Buckling Calculation and Summary Tables

Section 3 Brace End Connection Sample Calculation and Summary Tables

Section 4 Bottom Gusset Beam to Column Flange (Strong-Axis) Connection Sample
Calculation and Summary Tables

Section 5 Not used

Section 6 Not used

Section 7 Stiffness Sample Calculation and Summary Tables

Reed College Central Plant Upgrade

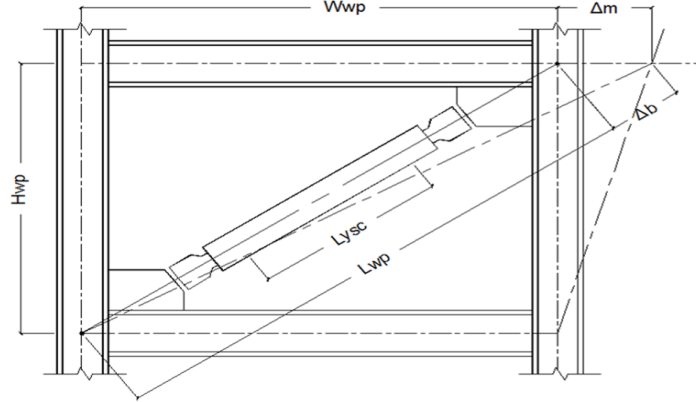
Calculation Submittal Package

Description

Section 1. Strain, β , and ω Determination and Submittal Tables

Strain and Overstrength Calculation

Example Mark #: 1901
Line 3+, Grid E.5-D.9, Level 2



1.0 DESIGN CRITERIA

Width Between Workpoints	W_{wp} :	88.00 in	(2235 mm)
Height Between Workpoints	H_{wp} :	121.93 in	(3097 mm)
Yielding Core Length	L_{ysc} :	69.29 in	(1760 mm)
Workpoint Length Along Diagonal $L_{wp} = \sqrt{(W_{wp}^2 + H_{wp}^2)}$	L_{wp} :	150.37 in	(3819 mm)
Yield Stress of Core Material for Establishing Area	F_{y-min} :	39 ksi	(269 MPa)
Maximum Yield Stress of Core Material	F_{y-max} :	46 ksi	(317 MPa)
Modulus of Elasticity	E:	29000 ksi	(199955 MPa)
LRFD Resistance Factor	ϕ_{BRB} :	0.90	
Deflection Amplification Factor	C_d :	5.00	
Demand Capacity Ratio	DCR:	1.00	
Importance Factor	I_E :	1.00	
Redundancy Factor	ρ :	1.00	
Specified Story Drift to Consider (Typically 1.0% Minimum unless NLRHA)	SSD:	1.00%	
<i>The displacements and strains associated with this value will later be multiplied by 2, so 2% minimum is typically being considered.</i>			
Area of Yielding Steel Core	A_{sc} :	4.00 in ²	(2581 mm ²)

1.1 STRAIN CALCULATION

Minimum Yield Force in Steel Core $(F_{y-min} \cdot A_{sc})$	$P_{ysc,min}$:	156 kip	(694 kN)
Maximum yield Force in Steel Core $(F_{y-max} \cdot A_{sc})$	$P_{ysc,max}$:	184 kip	(818 kN)
Final Width Between Workpoints after Specified Story Drift			
$W_f = W_{wp} + (SSD \cdot H_{wp})$	W_f :	89.22 in	(2266 mm)
$\Delta_{mSSD} = W_f - W_{wp}$ (for reference only)	Δ_{mSSD} :	1.22 in	(31 mm)
Final WP Length Along Diagonal After Specified Story Drift			
$L_f = \sqrt{(W_f^2 + H_{wp}^2)}$	L_f :	151.09 in	(3838 mm)
Yielding Core Elongation at Specified Story Drift $(L_f - L_{wp})$	Δ_{bSSD} :	0.72 in	(18 mm)
Core Strain at Considered Story Drift $(\Delta_{bSSD} / L_{ysc})$	ϵ_{bSSD} :	1.03%	
Core Strain at Design Story Drift $(C_d \cdot \text{Yield Strain})$			
Force for Elastic Drift Determination $P_d = \phi P_{ysc,min} / (\rho \cdot I) \cdot DCR$	P_d :	140 kip	(625 kN)
Stiffness of Yielding Core $K_{Lysc} = A_{sc} \cdot E / L_{ysc}$	K_{Lysc} :	1674 k/in	(293 kN/mm)
Core Deformation at Yield $\Delta_{by} = P_d / K_{Lysc}$	Δ_{by} :	0.08 in	(2 mm)
Core Deformation at Design Story Drift $\Delta_{bCd} = \Delta_{by} \cdot C_d$	Δ_{bCd} :	0.42 in	(11 mm)
Core Strain at Design Story Drift $\epsilon_{bCd} = \Delta_{bCd} / L_{ysc}$	ϵ_{bCd} :	0.61%	
<i>Note, identical results are found by calculating the strain with the following equation,</i>			
$\epsilon_{bCd} = \phi \cdot C_d \cdot (F_y / E) \cdot DCR / (I_E \cdot \rho)$, and then backing out the deformation, $\Delta_{bCd} = \epsilon_{bCd} \cdot L_{ysc}$			
$\Delta_{mCd} = \Delta_{bCd} / \cos(\tan^{-1}(H_{wp} / W_{wp}))$ (for reference only)	Δ_{mCd} :	0.72 in	(18 mm)
Required Stroke at Each End of Brace $(1/2 \text{ of } 2x \text{ Max of } \Delta_{bCd} \text{ \& } \Delta_{bSSD})$	$c_{req'd}$:	0.72 in	(18 mm)
Provided Stroke Distance at Each End of Brace	c :	3.00 in	(76 mm)

Controlling Strain (Max of ϵ_{bSSD} & ϵ_{bCd})

Strain at $2 \cdot \epsilon_{b,max}$

$\epsilon_{b,max}$: 1.03%

$2\epsilon_{b,max}$: 2.07%

1.2 DETERMINE OVERSTRENGTH FACTORS AT ϵ_{max} - SEE BACKBONE CURVES

Qualifying Similarity Test per AISC 341 K3.3

Yield Force of Test Specimen

Similarity (K3.3) Test: 10P

P_y : 86 kip (382 kN)

Test Extrapolation Range Downward per AISC 341-16

Minimum Qualified Yield Force

Extrapolation Downward 83%

$P_{y,min}$: 72 kip (318 kN)

Test Extrapolation Range Upward per AISC 341-16

Maximum Qualified Yield Force

Extrapolation Upward 333%

$P_{y,max}$: 286 kip (1273 kN)

Compression Strength Adjustment Factor at ϵ_{max}

$\beta_{K3.3}$: 1.19

Strain Hardening Adjustment Factor at ϵ_{max}

$\omega_{K3.3}$: 1.39

Qualifying Sub-Assemblage Test per AISC 341 K3.2

Yield Force of Test Brace

Subassemblage (K3.2) Test: 3P

P_y : 376 kip (1673 kN)

Compression Strength Adjustment Factor at ϵ_{max}

$\beta_{K3.2}$: 1.14

Strain Hardening Adjustment Factor at ϵ_{max}

$\omega_{K3.2}$: 1.35

Maximum Compression strength adjustment factor at ϵ_{max}

β_{max} : 1.19

Maximum Strain hardening adjustment factor at ϵ_{max}

ω_{max} : 1.39

These values may be increased for length effects where applicable. Design values may be larger.

Adjusted Brace Strength in Tension: $ABS_T = A_{sc} \cdot F_{y,max} \cdot \omega = P_{y,max} \cdot \omega$

P_{ut} : 255 kip (1134 kN)

Adjusted Brace Strength in Compression: $ABS_C = A_{sc} \cdot F_{y,max} \cdot \beta \cdot \omega = P_{y,max} \cdot \beta \cdot \omega$

P_{uc} : 304 kip (1353 kN)

1.3 BRACE ROTATIONAL DEMAND

2x Story Drift Rotation = $2 \cdot \text{MAX}(\Delta_{m1\%}, \Delta_{mCd})/H_{wd}$

$\delta = 2 \cdot \text{MAX}(\Delta_{mSSD}, \Delta_{mCd})/H_{wd}$ Equal to Assumed (Conservative) Translational Demand

δ : 0.02 rad

Assumed story drift rotation is considered conservative based on the following:

$\Delta_m = \delta \cdot H$ Maximum Story Drift for Project

$\Delta_t \leq \Delta_m$ $\delta_t = \Delta_t/L_{wd}$ Where Δ_t is the translation of the brace/beam joint and L_{wd} is the length of the brace

Δ_m : 2.44 in (62 mm)

$L_b \geq H$ Where H is the story height

$\Delta_m/H = \delta \cdot H/H = \delta = 0.02$ rad

Since $\Delta_t \leq \Delta_m$ and $L_b \geq H$ Then: $\Delta_t/L_b \leq \Delta_m/H \rightarrow \delta_t \leq \delta$

$\theta_{CB} = \tan^{-1}(H_{wd}/W_{wd})$ Angle between Horiz and BRB before rotation

θ_{CB} : 0.946 rad

$\Delta_t = \Delta_m \cdot \sin(\theta_{CB})$ Translation of brace/beam joint

Δ_t : 1.98 in (50 mm)

$\delta_t = \Delta_t/L_{wd}$ Rotational demand on BRB

δ_t : 0.013 rad

Alternate Method:

$\theta'_{CB} = \tan^{-1}(H_{wd}/(W_{wd} + \Delta_m))$ Angle between Horiz and BRB after rotation

θ'_{CB} : 0.933 rad

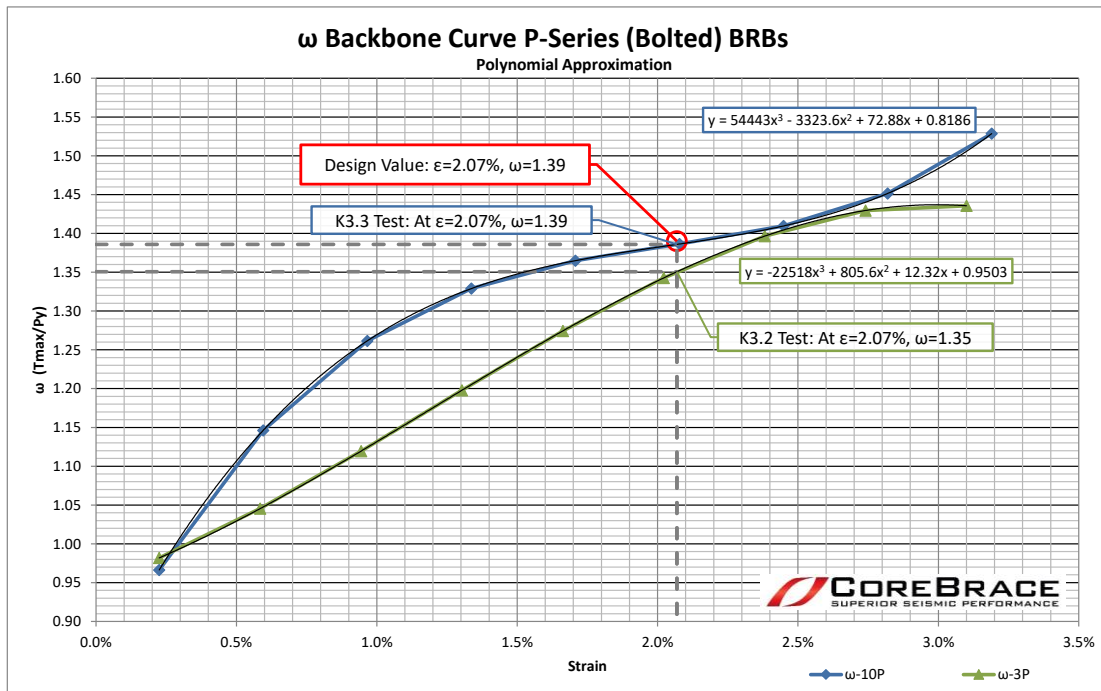
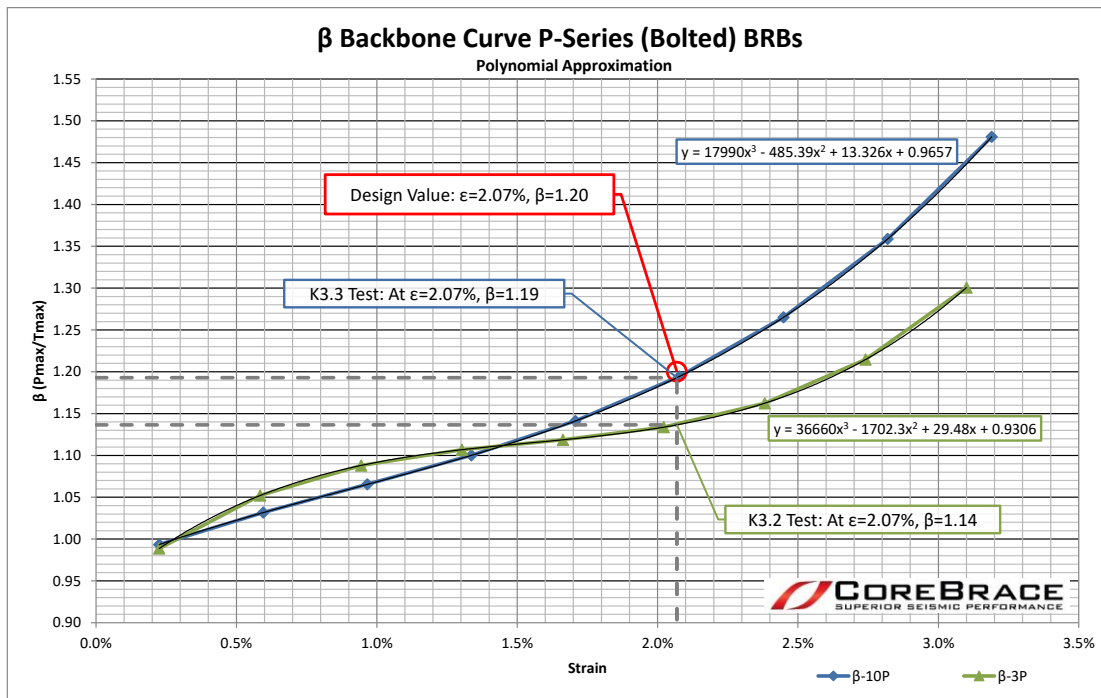
$\delta_{t-alt} = \theta_{CB} - \theta'_{CB}$

δ_{t-alt} : 0.013 rad

Therefore 0.02 Radians is Conservative

Tested Capacity from Test Report Must Equal 0.013 Radians. -- CoreBrace OK

1.4 BACKBONE CURVES





COREBRACE STRAIN CALCULATIONS

Project: Reed College Central Plant Upgrade

Location: Portland, OR

Job: 6903

Specimen ID and Location						SECTION 1.0 DESIGN CRITERIA														SECTION 1.1 STRAIN CALCULATION																
						Workpoint				Design Constant										Yield in Core		Story Drift										Strain				
EOR-ID #	Line	Grids #	Lvls #	Mark #	Qty #	W _{WP} in	H _{WP} in	L _{ysc} in	L _{WP} in	F _{ysc_min} ksi	F _{ysc_max} ksi	E ksi	ϕ _{BRB}	C _d	DCR	I	ρ	SSD %	A _{sc} in²	P _{ysc_min} kip	P _{ysc_max} kip	W _F in	Δ _{mSSD} in	L _F in	Δ _{bSSD} in	ε _{bSSD} %	P _d kips	K _{Lysc} k/in	Δ _{by} in	Δ _{bCd} in	ε _{bCd} %	Δ _{mCd} in	C _{req'd} in	C in	ε _{b,max} %	2ε _{b,max} %
BRB-4.00	3+	E.5-D.9	2	1901	1	88.0	121.9	69.3	150.4	39.0	46.0	29000	0.90	5.0	1.00	1.00	1.00	1.00%	4.00	156.0	184.0	89.2	1.22	151.1	0.72	1.03%	140	1674	0.08	0.42	0.61%	0.72	0.82	3.00	1.03%	2.07%
BRB-4.00	3+	E.5-D.9	1	1902	1	88.0	126.0	71.5	153.7	39.0	46.0	29000	0.90	5.0	1.00	1.00	1.00	1.00%	4.00	156.0	184.0	89.3	1.26	154.4	0.72	1.01%	140	1623	0.09	0.43	0.61%	0.76	0.83	3.00	1.01%	2.03%



COREBRACE STRAIN CALCULATIONS

Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

Specimen ID and Location						SECTION 1.2 DETERMINE OVERSTRENGTH FACTORS AT ϵ_{max}													SECTION 1.3 BRACE ROTATIONAL DEMAND						
						Axial Test Specimen per AISC 341 K3.3					Sub Test Specimen per AISC 341 K3.2				Design				Story Drift Rotation					Alt method	
EOR-ID #	Line	Grids #	Lvls #	Mark #	Qty #	Py kip	Test Specimen for "Py min" / "Py max"	Test Used	β	ω	Test Used	Py kip	β	ω	β	ω	P _{uT} kip	P _{uC} kip	δ_{rad}	Δ_m in	θ_{CB} rad	Δ_t in	δ_t rad	θ'_{CB} rad	δ_{t-alt} rad
BRB-4.00	3+	E.5-D.9	2	1901	1	85.82	10P / 10P	10P	1.19	1.39	3P	376.20	1.14	1.35	1.20	1.39	255.8	306.9	0.02	2.44	0.95	1.98	0.013	0.93	0.013
BRB-4.00	3+	E.5-D.9	1	1902	1	85.82	10P / 10P	10P	1.19	1.38	3P	376.20	1.13	1.34	1.19	1.38	253.9	302.2	0.02	2.52	0.96	2.07	0.013	0.95	0.013

Max

1.20

1.39

Reed College Central Plant Upgrade

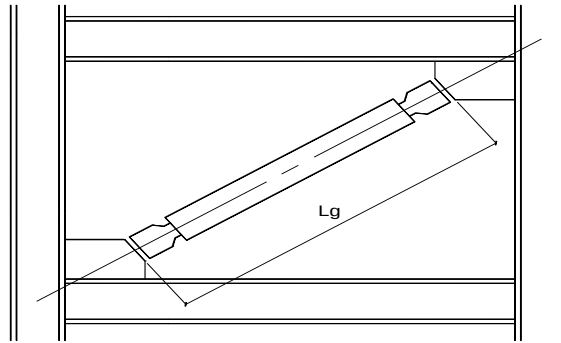
Calculation Submittal Package

Description

Section 2. Casing Buckling Calculations
Casing Buckling Summary Tables

Buckling Calculation

Example Mark #: 1901
Line 3+, Grid E.5-D.9, Level 2



2.0 DESIGN CRITERIA

Tip of gusset to tip of gusset is set as buckling length

Compression Strength Adjustment Factor

Strain Hardening Adjustment Factor

Upper Bound Yield Strength of Brace ($A_{sc} \cdot F_{y-max}$)

Upper Bound Yield Stress of Core Material

Area of Steel Core

Ultimate Load (Adjusted Brace Strength in Compression): $P_{uc} = (P_{y-sc-max} \cdot \beta \cdot \omega) = ABS_c$

Modulus of Elasticity

Model Brace as Pinned Both Ends (conservative)

Casing Moment of Inertia

t8x1/4

2.1 Euler Buckling

Solving Euler's buckling equation for required moment of inertia:

$$I_{lg} = \frac{FS_B \cdot P_{uc} \cdot (k \cdot L_{gg})^2}{\pi^2 E}$$

Where:

FS_B = Factor of Safety Against Buckling:
Verified by Testing

Unity Check:

L_{gg} : 115.13 in (2924 mm)

β : 1.2

ω : 1.39

$P_{y-sc-max}$: 184.0 kip (818 kN)

F_{y-max} : 46 ksi (317 MPa)

A_{sc} : 4.00 in² (2581 mm²)

P_{uc} : 306.9 kip (1365 kN)

E : 29000 ksi (199955 MPa)

k : 1.0

I_c : 70.7 in⁴ (2943 cm⁴)

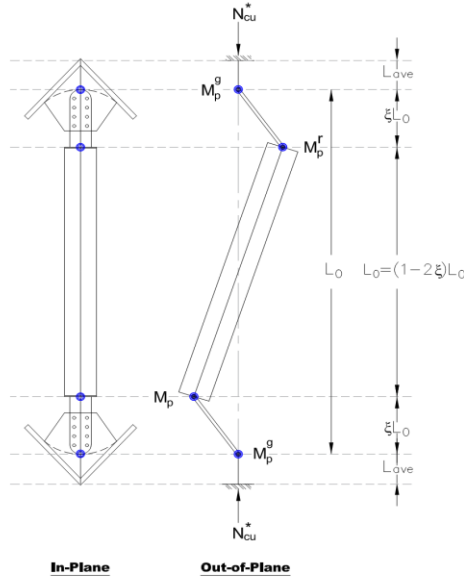
I_{lg} : 18.0 in⁴ (750 cm⁴)

FS_B : 1.27

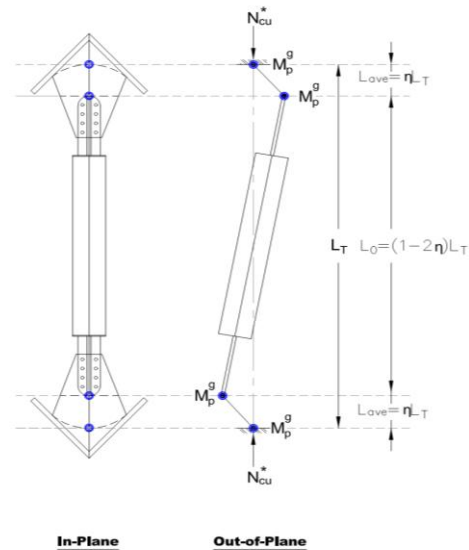
I_g/I_c : 0.25 OK

2.2 Global Stability (Notional Load Yield Line Method) - Asymmetrical Modes

See Zaboli (2018). Based on Takeuchi method - see references below.



Over-the-Yield Line (OYL) - Asymmetrical Mode



Under-the-Yield Line (UYL) - Asymmetrical Mode

2.2.1 NLYL Method Design Criteria

Overall Brace Length

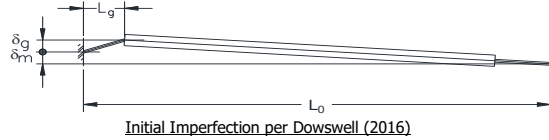
Additional Out-of-Plane Force on BRB (half assumed to go to each end):

Initial Imperfection of Neck Insertion Zone

Assumed Out-of-Plumbness of Brace: $\delta_m/L_0 = 1/x_{\delta m}$

Assumed Out-of-Flatness of Gusset Plate: $\delta_g/L_g = 1/x_{\delta g}$

Values of $x_{\delta m}$ and $x_{\delta g}$ per Dowswell (2016) recommendations. Imperfection of Neck per Takeuchi (2014).



Initial Imperfection per Dowswell (2016)

Critical Gusset Dimensions: Top Gusset

Top Gusset is Chev?

Top Gusset is Stiffened?

Is gusset stiffened sufficiently for K_b to be reduced? Can be "FALSE" even if stiffeners are present.

Stiffener Width

Stiffener Thickness

Gusset Thickness

Projected Stiffener Plastic Section Modulus (Proj per Dowswell. All stiff's combined.)

Yield Strength of Gusset Material

Length from WL Intersection w/Beam or Col along WL to Tip of Brace

Clear from Col to Lug Edge

Clear from Beam to Lug Edge

Controlling Bendline Length, Gusset Edge to Brace Tip:

Bm Side

Col Side

Chev_{Top}:

FALSE

Stiff_{Top}:

FALSE

W_{stiff,top}:

-

-

t_{stiff,top}:

-

-

t_{a,top}:

1.00 in

(25 mm)

Z_{stiff,top}:

-

-

F_{y,top}:

50 ksi

(345 MPa)

a_{top}:

5.66 in

(144 mm)

b_{top}:

1.09 in

(28 mm)

c_{top}:

4.91 in

(125 mm)

L_{b,top}:

12.26 in

(311 mm)

L_{c,top}:

13.04 in

(331 mm)

Critical Gusset Dimensions: Bottom Gusset

Bottom Gusset is Chev?

Bottom Gusset is Stiffened?

Is gusset stiffened sufficiently for K_b to be reduced? Can be "FALSE" even if stiffeners are present.

Stiffener Width

Stiffener Thickness

Gusset Thickness

Projected Stiffener Plastic Section Modulus (Proj per Dowswell. All stiff's combined.)

V_{Bot}:

FALSE

Stiff_{Bot}:

FALSE

W_{stiff,bot}:

-

-

t_{stiff,bot}:

-

-

t_{a,bot}:

1.00 in

(25 mm)

Z_{stiff,bot}:

-

-

Yield Strength of Gusset Material	$F_{y,bot}$	50 ksi	(345 MPa)
Length from WL Intersection w/Beam or Col along WL to Tip of Brace	a_{bot}	5.79 in	(147 mm)
Clear from Col to Lug Edge	b_{bot}	1.17 in	(30 mm)
Clear from Beam to Lug Edge	c_{bot}	4.61 in	(117 mm)
Controlling Bendline Length, Gusset Edge to Brace Tip:	$L_{b,bot}$	12.31 in	(313 mm)
	$L_{c,bot}$	12.97 in	(329 mm)
Core Dimensions and Properties			
Ultimate Stress of Core Material	F_{usc}	66 ksi	(455 MPa)
Core Width at Neck Section	W_t	4.00 in	(102 mm)
Core Thickness	t_c	1.00 in	(25 mm)
Neck Insertion Length for Out-of-Plane Buckling Direction	L_{in}	9.73 in	(247 mm)
Note that $L_{in}/W_t = \text{Embedment Ratio} = 2.43$			
Lug and Bolt Pattern Dimensions			
Width of Lug Plate	W_L	7.50 in	(191 mm)
Width of Lug at Neck Section	W_1	4.98 in	(127 mm)
Length of Lug on Gusset Measured to Square Projection	L'_{Lg}	11.25 in	(286 mm)
Transition Length, W_L to W_1	a	4.00 in	(102 mm)
Stroke Length, End of Transition to Casing	c	3.00 in	(76 mm)
Lug Thickness	t_L	0.63 in	(16 mm)
Yield Strength of Lug Material	F_{yL}	50 ksi	(345 MPa)
Ultimate Strength of Lug Material	F_{uL}	65 ksi	(448 MPa)
Number of Bolts in Inner Row Along Brace Axis	n_i	3	
Number of Bolts in Outer Row Along Brace Axis	n_o	0	
Bolt Spacing	s	4.00 in	(102 mm)
Plate Edge to CL of Bolt	e_{perp}	1.63 in	(41 mm)
Restrainer (Casing) Size and Properties			
Restrainer Section Name	Section:	t8x1/4	
Yield Stress of Casing Material	F_{yc}	46 ksi	(317 MPa)
Youngs Modulus of Casing Material	E_c	29000 ksi	(199955 MPa)
Casing is Square/Rectangular?	Sq_{Cas}	TRUE	
Casing Height (Dimension Viewed in Elevation)	H_c	8.00 in	(203 mm)
Casing Width (Dimension Viewed in Plan & Overall Dimension for p Sections)	W_c	8.00 in	(203 mm)
Casing Thickness	t_c	0.25 in	(6 mm)
Factor on Adjusted Brace Strength	F_{PUC}	1.0	
Capacity Reduction Factor, ϕ_{NLYL}	ϕ_{NLYL}	1.0	
Equal to 1.0 per Takeuchi (2014). Lower values can be used.			
Zaboli (2018) is even more conservative than Takeuchi even with $\phi = 1.0$.			

2.2.2 NLYL Global Stability Method

Overstrength Compression Force in the Core of the BRB: $N_{cu}^* = F_{Pu} \cdot P_{UC}$	N_{cu}^*	306.9 kip	(1365 kN)
NLYL Method Uses: $N_{cu}^* = \text{Overstrength Compression Capacity of the BRB. This requires an iterative solution.}$			
The variant used here checks demand vs capacity based on applied load (P_u).			
Length from End of Casing to Yield Line at Tip of Brace: $\xi_{L0} = a + c + L'_{LG}$	ξ_{L0}	18.25 in	(464 mm)
Destabilizing Factor for OYL Method: $\xi = \xi_{L0}/L_0$	ξ	0.146	
Effective Length Factor for Brace including Gusset Stiffness Effect: k_b	k_b	1.00	
If $Stiff_{Top}$ AND $Stiff_{Bot} = \text{TRUE}$, $k_b = 0.7$			
If $Stiff_{Top}$ AND $Stiff_{Bot} = \text{FALSE}$, $k_b = 1.0$			
If $Stiff_{Top}$ OR $Stiff_{Bot} = \text{FALSE}$, $k_b = 0.85$			
Stiffened Gusset Factor, $\lambda = 1.19$ for Stiffened Gusset or 1.0 for Unstiffened Gusset	λ_{top}	1.00	
	λ_{bot}	1.00	
Global Elastic Buckling Capacity of BRB, Incl Effect of Gusset PL: $N_{cr}^B = \pi^2 \cdot EI / (k_b \cdot L_0)^2$	N_{cr}^B	1289.9 kip	(5738 kN)
Effective Width in Compression: $b_{ga} = 2 \cdot L_{Br} \cdot \tan(\theta_{disp}) + (W_L - 2 \cdot e_{perp})$	L_{Br}	8.00 in	(203 mm)
Lug Lap on Gusset: $L_{Br} = IF(n_i > n_o, (n_i - 1) \cdot s, (n_o - 0.5) \cdot s)$	$\theta_{disp, top}$	40.0°	
Dispersion Angle at Top Gusset	$\theta_{disp, bot}$	40.0°	
Dispersion Angle at Bottom Gusset	Dispersion angle based on 30° for V or Chev, 40° otherwise per NLYL Methodology.		
Effective Compression Width, Top Gusset	$b_{ga, top}$	17.68 in	(449 mm)
Effective Compression Width, Bottom Gusset	$b_{ga, bot}$	17.68 in	(449 mm)
Average Gusset Buckling Length: $L_{ave} = \min[(a + \min(b, c))/2, (a + b + c)/3]$	$L_{ave, top}$	3.38 in	(86 mm)
See Dowswell (2006) and Zaboli (2018)	$L_{ave, bot}$	3.48 in	(88 mm)
Nominal Axial Capacity of Gusset Plate: $N_s^g = b_{ga} \cdot t_g \cdot F_{yG}$	$N_{s, top}^g$	883.8 kip	(3931 kN)
	$N_{s, bot}^g$	883.8 kip	(3931 kN)

Euler Buckling Capacity of Gusset Plate: $N_e = \pi^2 \cdot E \cdot (b_{aa} \cdot t_g^3 / 12) / L_{ave}^2$

$N_{e,top}:$ **36952.6 kip** (164372 kN)
 $N_{e,bot}:$ **34824.2 kip** (154905 kN)

Plastic Moment Capacity of Gusset Plates

Total Bendline Length: $b_{gf} = L_b + L_c$

Plastic Section Modulus: $Z_g = b_{gf} \cdot t_g^2 / 4 + Z_{stiff}$

Plastic Moment Capacity: $M_{zy}^g = Z_g \cdot F_{vg}$

$b_{gf,top}:$ 25.30 in (643 mm)
 $b_{gf,bot}:$ 25.27 in (642 mm)
 $Z_{g,top}:$ 6.32 in³ (103642 mm³)
 $Z_{g,bot}:$ 6.32 in³ (103536 mm³)
 $M_{zy,top}^g:$ **316 k-in** (35.7 kN-m)
 $M_{zy,bot}^g:$ **316 k-in** (35.7 kN-m)

Reduced Plastic Moment Capacity of Gusset Plate Including Axial Force Effect:

$M_p^g = \lambda \cdot \phi_{NLVL} \cdot M_{zy}^g [1 - (N^*_{cu} / (\phi_{NLVL} \cdot N^g_{sy}))^2] \geq 0$

$M_{p,top}^g:$ 278 k-in (31.4 kN-m)
 $M_{p,bot}^g:$ 278 k-in (31.4 kN-m)

Axial Yield Strength of Neck at Web Zone: $N^0_{wy} = 2 \cdot (W_1 - t_{sc}) \cdot t_l \cdot F_{vL}$

Axial Yield Strength of Neck: $N^0_v = W_t \cdot t_{sc} \cdot F_{vmax} + 2 \cdot (W_1 - t_{sc}) \cdot t_l \cdot F_{vL}$

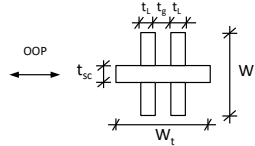
Axial Ultimate Strength of Neck: $N^0_u = W_t \cdot t_{sc} \cdot F_{u,sc} + 2 \cdot (W_1 - t_{sc}) \cdot t_l \cdot F_{uL}$

$N^0_{wy}:$ 248.9 kip (1107 kN)
 $N^0_v:$ 432.9 kip (1926 kN)
 $N^0_u:$ 587.5 kip (2613 kN)

OOP Plastic Section Modulus of Steel Core (W_t) at Neck Section: $Z_{Wt,oop} = t_{sc} \cdot W_t^2 / 4$

OOP Plastic Section Modulus of Lugs (W_1) at Neck Sect: $Z_{W1,oop} = [W_1 \cdot t_{sc}] \cdot ((2 \cdot t_l + t_{sc})^2 - t_{sc}^2) / 4$

$Z_{Wt,oop}:$ 4.0 in³ (65548 mm³)
 $Z_{W1,oop}:$ 4.0 in³ (66273 mm³)



Section at Neck

Out-of-Plane Plastic Moment Capacity of Neck: $M^0_{zy} = Z_{Wt,oop} \cdot F_{vmax} + Z_{W1,oop} \cdot F_{vL}$

$M^0_{zy}:$ **386 k-in** (43.6 kN-m)

Reduced Restrainer Moment Transfer Capacity Determined by Neck + Core Plate, Including Axial Force Effect.

$M_{o,r-neck} = \phi_{NLVL} \cdot M^0_{zy} \cdot [1 - (N^*_{cu} / (\phi_{NLVL} \cdot (N^0_u)^{exp}))]$

Exponent, $exp = 2.0$

Use N^0_v if Gst is Not Stiffened?

FALSE

Per Takeuchi (2014), N^0_u is used in the denominator. Other methods use N^0_v in the denominator if the gusset is unstiffened.

$M_{o,r-neck,top}:$ 280.8 k-in (31.7 kN-m)
 $M_{o,r-neck,bot}:$ 280.8 k-in (31.7 kN-m)

Plastic Section Modulus of Restrainer, Z_{r0}

Square / Rectangular Section: $Z_{r0} = H_c \cdot W_c^2 / 4 - (H_c - 2 \cdot t_c) \cdot (W_c - 2 \cdot t_c)^2 / 4$

Round Casing Section: $Z_{r0} = W_c^3 / 6 - (W_c - 2 \cdot t_c)^3 / 6$

$Z_{r0}:$ 22.5 in³ (369221 mm³)

Nominal Plastic Moment Capacity of Restrainer: $M^i_{zy} = Z_{r0} \cdot F_{vc}$

$M^i_{zy}:$ 1036 k-in (117.1 kN-m)

Embed Length Calibration Factor: $\alpha'_p = 4.15 - 1.5 \cdot (L_{in} / W_t) = 4.15 - 1.5 \cdot L_{in} / W_t \geq 1.5$

See Takeuchi (2014). While this increases as embedment ratio (L_{in} / W_t) decreases, the net effect of a decreasing embedment ratio decreases $M_{o,r-neck}$, and this factor only slows the decrease.

$\alpha'_p:$ 1.50

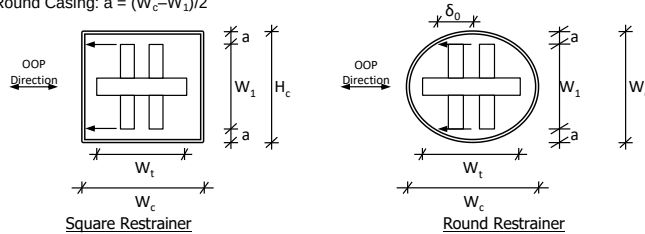
Distance between the shear force application point and the outer surface of the restraint tube, a

See Matsui (2010) for calculation of square and round restrainer properties.

Sq/Rect Casing: $a = (H_c - W_1) / 2$

Round Casing: $a = (W_c - W_1) / 2$

$a:$ 1.51 in (38 mm)



Distance between the Core Plate Surface and the Shear Force Application Point when the Shear Force is not Present, δ_0 . Not Applicable to Square/Rect Restrainers.

See Matsui (2010) and Takeuchi (2017). Eqn from Takeuchi (2017) Ch 4

$\delta_0 = W_d / 2 \cdot \sin[\cos^{-1}((W_c - 2 \cdot a) / (W_c - 2 \cdot t_c))]$

$\delta_0:$ 2.99 in (76 mm)

The Lateral Deflection of the Restrainer Tube at the In-Plane Stress Yielding. Not Applicable to Square/Rect Restrainers.

See Matsui (2010) and Takeuchi (2017). Eqn from Takeuchi (2017) Ch 4

$\delta_y = \sqrt{[(\pi \cdot W_c \cdot F_{vc} / (4 \cdot E_d) + W_d / 2 \cdot \cos^{-1}((W_c - 2a) / (W_c - 2t_c)))^2 - a^2]}$

$\delta_y:$ 3.03 in (77 mm)

Elastic Rotational Stiffness of Restrainer about Rib End:

$$\text{Round Casing: } K_{Rr1, \text{Round}} = 2 \cdot F_{vc} \cdot t_c \cdot L_{in}^3 / (3 \cdot \sqrt{a^2 + \delta_v^2}) \cdot \delta_v / (\delta_v - \delta_0) \geq 0$$

$$K_{Rr1, \text{Round}}: \frac{148989 \text{ k-in}}{\text{rad}} \quad (1.68E+04 \text{ kN-m})$$

$$\text{Square/Rect Casing: } K_{Rr1, \text{Rect}} = E_c \cdot H_c \cdot t_c^3 \cdot L_{in}^3 / (3 \cdot (2 \cdot H_c \cdot a^3 - 3 \cdot a^4)) \geq 0$$

$$K_{Rr1, \text{Rect}}: \frac{28213 \text{ k-in}}{\text{rad}} \quad (3.19E+03 \text{ kN-m})$$

Post-Yielding Rotational Stiffness of Restrainer about Rib End:

$$\text{Round Casing: } K_{Rr2, \text{Round}} = 0$$

$$\text{Square/Rect Casing: } K_{Rr2, \text{Rect}} = 0.11 \cdot F_{vc} \cdot H_c^3 \cdot (L_{in}/W_r)^3 \geq 0$$

$$K_{Rr2, \text{Rect}}: \frac{37260 \text{ k-in}}{\text{rad}} \quad (4.21E+03 \text{ kN-m})$$

Yield Angle of Circular Casing: $\theta_{v, \text{Round}} = (\delta_v - \delta_0) / L_{in}$

$$\theta_{v, \text{Round}}: 0.004359 \text{ rad}$$

Pseudo Initial Yield Angle of the Rect Casing: $\theta'_{v1} = 0.00164 \cdot (F_{vc}/E_{casing}) \cdot (H_c/t_c) \cdot (W_r/L_{in})$

$$\theta'_{v1}: 0.000034 \text{ rad}$$

Angle at Which Plastic Hinge Occurs: $\theta_{v2} = H_c/L_{in} \cdot \sqrt{[(F_{vc}/(2 \cdot E_{casing}))^2 + (a \cdot F_{vc}/(H_c \cdot E_{casing}))]}$

$$\theta_{v2}: 0.014240 \text{ rad}$$

See Matsui (2010) and Takeuchi (2017) ch 4

Reduced Restrainer Moment Transfer Capacity Determined by Restrainer Section at Rib:

$$\text{Round Casing: } M_o^{r-\text{rest}} = \text{MIN}[M'_{zv}, \sigma'_n \cdot K_{Rr1, \text{Round}} \cdot \theta_{v, \text{Round}}]$$

$$M_o^{r-\text{rest}}: 795 \text{ k-in} \quad (89.9 \text{ kN-m})$$

$$\text{Square/Rect Casing: } M_n^{r-\text{rest}} = \text{MIN}[M'_{zv}, \sigma'_n \cdot (K_{Rr1, \text{Rect}} \cdot \theta'_{v1} + K_{Rr2, \text{Rect}} \cdot (\theta_{v2} - \theta'_{v1}))]$$

Controlling Restrainer Moment Transfer Capacity: $M_p^r = \text{Min}\{M_p^{r-\text{neck}}, M_p^{r-\text{top}}, M_p^{r-\text{rest}}\}$

Top End of Brace Controlled By: **Neck Capacity**

Bottom End of Brace Controlled By: **Neck Capacity**

$$M_{p, \text{top}}^r: 280.8 \text{ k-in} \quad (31.7 \text{ kN-m})$$

$$M_{p, \text{bot}}^r: 280.8 \text{ k-in} \quad (31.7 \text{ kN-m})$$

2.2.3 Over the Yield Line (OYL) Global Buckling Capacity

Total Initial Imperfection with Plastic Hinge at End of Casing: $\theta_{i, \text{OYL}}$

$$\theta_{i, \text{OYL}}: 0.0171 \text{ rad}$$

$$\theta_{i, \text{OYL}} = \delta_m/L_0 + \delta_d/L_0 + \theta_0$$

Moment Amplification Factor to Account for 2nd Order Effects: $\delta_{s, \text{OYL}}$

$$\delta_{s, \text{OYL}}: 1.3122$$

$$\delta_{s, \text{OYL}} = 1/(1 - N_{cu}^*/N_{cr}^B) \geq 1.0$$

Reports as "Error" if result is less than 1.0, which occurs when applied load (N_{cu}^*) exceeds BRB elastic buckling capacity (N_{cr}^B).

Notional Load Applied at Brace End: $N_{\text{OYL}} = N_{cu}^* \cdot \theta_{i, \text{OYL}} + F_{\text{Add1-OOP}}/2$

$$N_{\text{OYL}}: 5.3 \text{ kip} \quad (23 \text{ kN})$$

$$N \xi L_0 \delta_s \leq (1 - 2\xi) M_p^g + M_p^r \quad \text{Iterative Solution}$$

$$\frac{N \xi L_0 \delta_s}{(1 - 2\xi) M_p^g + M_p^r} \leq 1.0 \quad \text{DCR}$$

Demand: $D = N_{\text{OYL}} \xi L_0 \delta_{s, \text{OYL}}$

$$D: 126.0 \text{ k-in} \quad (14.2 \text{ kN-m})$$

Capacity: $C_{\text{top}} = (1 - 2\xi) M_{p, \text{top}}^g + M_{p, \text{top}}^r$

$$C_{\text{top}}: 477.9 \text{ k-in} \quad (54.0 \text{ kN-m})$$

$$C_{\text{bot}} = (1 - 2\xi) M_{p, \text{bot}}^g + M_{p, \text{bot}}^r$$

$$C_{\text{bot}}: 477.7 \text{ k-in} \quad (54.0 \text{ kN-m})$$

Stability Index (SI): $D/C_{\text{OYL}} = D/[\text{min}\{C_{\text{top}}, C_{\text{bot}}\}]$

$$SI_{\text{OYL}}: 0.26 \quad \text{OK}$$

2.2.4 Under the Yield Line (UYL) Global Buckling Capacity

Total Initial Imperfection with Plastic Hinge at End of Casing: $\theta_{i, \text{UYL}}$

$$\theta_{i, \text{UYL}}: 0.0271 \text{ rad}$$

$$\theta_{i, \text{UYL}} = \delta_m/L_0 + 2 \cdot \delta_d/L_0 + \theta_0$$

Moment Amplification Factor to Account for 2nd Order Effects: $\delta_{s, \text{UYL}}$

$$\delta_{s, \text{UYL, top}}: 1.008$$

$$\delta_{s, \text{UYL, top}} = 1/(1 - N_{cu}^*/N_{e, \text{top}}) \geq 1.0$$

$$\delta_{s, \text{UYL, bot}}: 1.009$$

$$\delta_{s, \text{UYL, bot}} = 1/(1 - N_{cu}^*/N_{e, \text{bot}}) \geq 1.0$$

Reports as "Error" if result is less than 1.0, which occurs when applied load (N_{cu}^*) exceeds gusset elastic buckling capacity (N_e).

Notional Load Applied at Brace End: $N_{\text{UYL}} = N_{cu}^* \cdot \theta_{i, \text{UYL}} + F_{\text{Add1-OOP}}/2$

$$N_{\text{UYL}}: 8.3 \text{ kip} \quad (37 \text{ kN})$$

Total Length, $L_T = L_{\text{ave, bot}} + L_0 + L_{\text{ave, top}}$

$$L_T: 132.11 \text{ in} \quad (3356 \text{ mm})$$

Destabilizing Factor for UYL Method: $\eta = (1 - L_0/L_T)/2$

$$\eta: 0.026$$

$$N L_{\text{ave}} \delta_s \theta = (2 - 2\eta) M_p^g \Rightarrow M_p^g \geq \frac{N L_{\text{ave}} \delta_s}{(2 - 2\eta)} = M_y^*$$

Iterative Solution

$$\frac{M_y^*}{M_p^g} \leq 1.0 \quad \text{Stability Index (SI)}$$

$$M_{y, \text{top}}^* = N_{\text{UYL}} \cdot L_{\text{ave, top}} \cdot \delta_{s, \text{UYL, top}} / (2 - 2\eta)$$

$$M_{y, \text{top}}^*: 14.6 \text{ k-in} \quad (1.6 \text{ kN-m})$$

$$M_{y, \text{bot}}^* = N_{\text{UYL}} \cdot L_{\text{ave, bot}} \cdot \delta_{s, \text{UYL, bot}} / (2 - 2\eta)$$

$$M_{y, \text{bot}}^*: 15.0 \text{ k-in} \quad (1.7 \text{ kN-m})$$

$$\text{DCR} = \max\{M_{y, \text{top}}^*/M_{p, \text{top}}^g, M_{y, \text{bot}}^*/M_{p, \text{bot}}^g\}$$

$$SI_{\text{top}}: 0.05 \quad \text{OK}$$

$$SI_{\text{bot}}: 0.05 \quad \text{OK}$$

$$SI_{\text{UYL}}: 0.05 \quad \text{OK}$$

Interaction Equation Form of General Solution:

$$\left(\frac{N_{cu}^*}{\phi N_s^g}\right)^2 + \frac{M_y^*}{\lambda \phi M_{zy}^g} \leq 1$$

Interaction Equation

Interaction equation will produce results that equal 1.0 at for same value of N*cu as the UYL DCR equation but it is less sensitive (less volatile) to small changes in N*cu. Neither the DCR nor the Int Egn produces results that are linear with respect to N*cu (i.e. a Int Egn value = 0.5 is not capable of handling 2x N*cu). An interaction eqn solution is not possible for the OYL method.

Int _{top} :	0.17	OK
Int _{bot} :	0.17	OK
Int _{UYL} :	0.17	OK

2.2.5 NLYL Summary

Global stability in the Asymmetrical Mode is controlled by the lesser of the capacities determined by the OYL and UYL methods.

OYL:	SI _{OYL} :	0.26	OK
UYL:	SI _{UYL} :	0.05	OK
UYL _{INT} :	Int _{UYL} :	0.17	OK

Summary:	OK
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2.2.6 References

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Takeuchi, T. Ozaki, H. Matsui, R. & Sutcu, F. (2014), Out-of-plane stability of buckling-restrained braces including moment transfer capacity, Earthquake Engineering & Structural Dynamics, 43(6), 851-869

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Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

CASING BUCKLING CALCULATIONS

Specimen ID and Location						Casing Profile				Section 2.0 Design Criteria												Section 2.1 Euler Buckling		Section 2.2.1 NLVL Method Design Criteria																	
																								Overall Brace Length									Critical Gusset Dimensions for Top Gusset								
EOR-ID	Line	Grids	Lvls	Mark	Qty	Type	H _c	W _c	t _c	L _{ss}	β	ω	P _{ysc,max}	F _{ysc,max}	A _{sc}	P _{uc}	E	k	I _c	I _g	FS	I _g '	L ₀	F _{Addl-OOP}	θ ₀	δ _m /L ₀	δ _g /L _g	Is Chev Top T/F	Stiffened Gusset Top T/F	W _{stiff,g,top}	t _{stiff,g,top}	t _{g,top}	Z _{g,top}	F _{yg,top}	a _{top}	b _{top}	c _{top}	L _{0,top}	L _{c,top}		
#			#	#	#		in	in	in	in			kips	ksi	in²	kips	ksi			in⁴	in⁴	Buckling	I _c	in	kip	rad	rad	rad			in	in	in	in³	ksi	in	in	in	in	in	in
BRB-4.00	3+	E.5-D.9	2	1901	1	t	8	8	0.2500	115.13	1.20	1.39	184	46.0	4.0	307	29000	1.0	70.7	18.0	1.27	0.25	125.3	0.0	0.005	0.002	0.010	FALSE	FALSE	-	-	1.0	6.3	50	5.7	1.1	4.9	12.3	13.0		
BRB-4.00	3+	E.5-D.9	1	1902	1	t	8	8	0.2500	117.13	1.19	1.38	184	46.0	4.0	302	29000	1.0	70.7	18.4	1.27	0.26	127.3	0.0	0.005	0.002	0.010	FALSE	FALSE	-	-	1.0	6.3	50	5.7	1.0	4.8	12.3	12.8		

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Location: Portland, OR
Job: 6903

CASING BUCKLING CALCULATIONS

Specimen ID and Location						Section 2.2.1 NLYL Method Design Criteria														Section 2.2.1 NLYL Method Design Criteria														
						Critical Gusset Dimensions for bottom Gusset												Core Dimensions and Properties						Lug and Bolt pattern Dimensions										
EOR-ID	Line	Grids	Lvls	Mark	Qty	Is V Bot T/F	Stiffened Gusset Bot T/F	W _{stiff,g,bot} in	t _{stiff,g,bot} in	t _{g,bot} in	Z _{g,bot} in³	F _{yg,bot} ksi	a _{bot} in	b _{bot} in	c _{bot} in	L _{u,bot} in	L _{c,bot} in	F _{usc} ksi	W _t in	t _{sc} in	L _{in} in	OOP Embed Ratio	W _L in	W ₁ in	L' _{Lg} in	a in	c in	t _L in	F _{yk} ksi	F _{uL} ksi	n _l #	n _o #	s in	e _{perp} in
BRB-4.00	3+	E.5-D.9	2	1901	1	FALSE	FALSE	-	-	1.0	6.3	50.0	5.8	1.2	4.6	12.3	13.0	66.0	4.0	1.000	9.7	2.4	7.5	5.0	11.3	4.0	3.0	0.6	50.0	65.0	3	0	4.0	1.6
BRB-4.00	3+	E.5-D.9	1	1902	1	FALSE	FALSE	-	-	1.0	7.2	50.0	6.8	1.6	7.2	13.8	14.9	66.0	4.0	1.000	9.6	2.4	7.5	4.9	11.3	4.0	3.0	0.6	50.0	65.0	3	0	4.0	1.6

CASING BUCKLING CALCULATIONS

Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

Specimen ID and Location						Section 2.2.1 NLYL Method Design Criteria								Section 2.2.2 NLYL Global Stability Method																Section 2.2.2 NLYL Global Stability Method																			
						Casing Size and Properties						Strength Factors		General Design Parameters										Gusset Capacity								Restrainer Capacity Based on Moment Capacity of Neck																	
EOR-ID	Line	Grids	Lvls	Mark	Qty	Casing Size	F _{yc} ksi	E _{casing} ksi	Casing is Sq/Rect?	H _c in	W _c in	t _c in	F _{PRC}	φ	N _{cu} [*] kip	ξ _{Lo} in	ξ	λ _{top}	λ _{bot}	N _{cr} ^A kip	L _{Dr} in	θ _{dis, top} degree	θ _{dis, bot} degree	b _{ga, top} in	b _{ga, bot} in	L _{ave, top} in	L _{ave, bot} in	N _{s, top} ^B kip	N _{s, bot} ^B kip	N _{e, top} kip	N _{e, bot} kip	b _{gf, top} in	b _{gf, bot} in	Z _{g, top} in³	Z _{g, bot} in³	M _{zy, top} ^C kip-in	M _{zy, bot} ^C kip-in	M _{p, top} ^E kip-in	M _{p, bot} ^E kip-in	N _{wy} ^F kip	N _y ^F kip	N _u ^F kip	Z _{WT} in³	Z _{W1} in³	M _{zy} ^G kip-in	M _{p, neck, top} ^H kip-in	M _{p, neck, bot} ^H kip-in		
		#	#	#	#																																												
BRB-4.00	3+	E.5-D.9	2	1901	1	t8x1/4	46.0	29000	TRUE	8.0	8.0	0.25	1.00	1.0	307	18.25	0.15	1.00	1.00	1290	8.0	40	40	17.7	17.7	3.4	3.5	884	884	36953	34824	25.3	25.3	6.32	6.32	316	316	278	278	249	433	588	4.00	4.04	386	281	281		
BRB-4.00	3+	E.5-D.9	1	1902	1	t8x1/4	46.0	29000	TRUE	8.0	8.0	0.25	1.00	1.0	302	18.25	0.14	1.00	1.00	1250	8.0	40	40	17.7	17.7	3.4	4.2	884	884	37402	23987	25.0	28.8	6.26	7.19	313	360	276	318	244	428	581	4.00	3.97	382	279	279		

CASING BUCKLING CALCULATIONS

Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

Specimen ID and Location						Section 2.2.2 NLVL Global Stability Method															Section 2.2.3 Over the Yield Line (OYL) Global Buckling Capacity										Section 2.2.4 Under the Yield Line (UYL) Global Buckling Capacity										Section 2.2.5						
						Restrainer Capacity Based on Mom Txfr Cap of Rest															Controlling Rest Cap					Over the Yield Line Buckling (Asymm Mode)					Under the Yield Line Buckling (Asymm Mode)					Demand Capacity Ratio										Interaction Equation	
EOR-ID	Line	Grids	Lvls	Mark	Qty	Z _p	M' _{zy}	α' _p	a	δ ₀	δ _y	K _{R1,Round}	K _{R1,Rect}	K _{R2,Rect}	θ _{y,Round}	θ' _{y1}	θ _{y2}	M _p ^{rest}	M' _{p,bot}	M' _{p,top}	θ _{1,OYL}	δ _{1,OYL}	N _{OYL}	Stability Index Max OYL	Demand	Capacity _{top}	Capacity _{bot}	Stability Index OYL	θ _{1,UYL}	δ _{s,UYL,bot}	δ _{s,UYL,top}	N _{UYL}	L _T	η	M* _{y,top}	M* _{y,bot}	Stability Index Top	Stability Index Bot	Stability Index UYL	Int _{top}	Int _{bot}	Int _{UYL}	S _{OYL}	S _{UYL}	Int _{UYL}	Check ≤ 1	
						in ³	kip-in		in	in	in	(k-in)/rad	(k-in)/rad	(k-in)/rad	rad	rad	rad	kip-in	kip-in	kip-in	rad	M Mag factor	kip	kip-in	kip-in	kip-in		kip	kip	kip	kip	in		kip-in	kip-in												OK/NG
BRB-4.00	3+	E.5-D.9	2	1901	1	22.5	1036	1.50	1.51	2.99	3.03	148989	28213	37260	0.0044	0.000034	0.0142	795	281	281	0.017	1.31	5.3	0.26	126.0	477.9	477.7	0.3	0.03	1.01	1.01	8.3	132.1	0.03	14.6	15.0	0.05	0.05	0.05	0.2	0.2	0.2	0.26	0.05	0.17	OK	
BRB-4.00	3+	E.5-D.9	1	1902	1	22.5	1036	1.50	1.55	3.03	3.07	126682	25621	36153	0.0050	0.000035	0.0146	789	279	279	0.017	1.32	5.2	0.26	125.0	476.1	505.5	0.3	0.03	1.01	1.01	8.2	134.8	0.03	14.3	17.9	0.05	0.06	0.06	0.2	0.2	0.2	0.26	0.06	0.17	OK	

Reed College Central Plant Upgrade

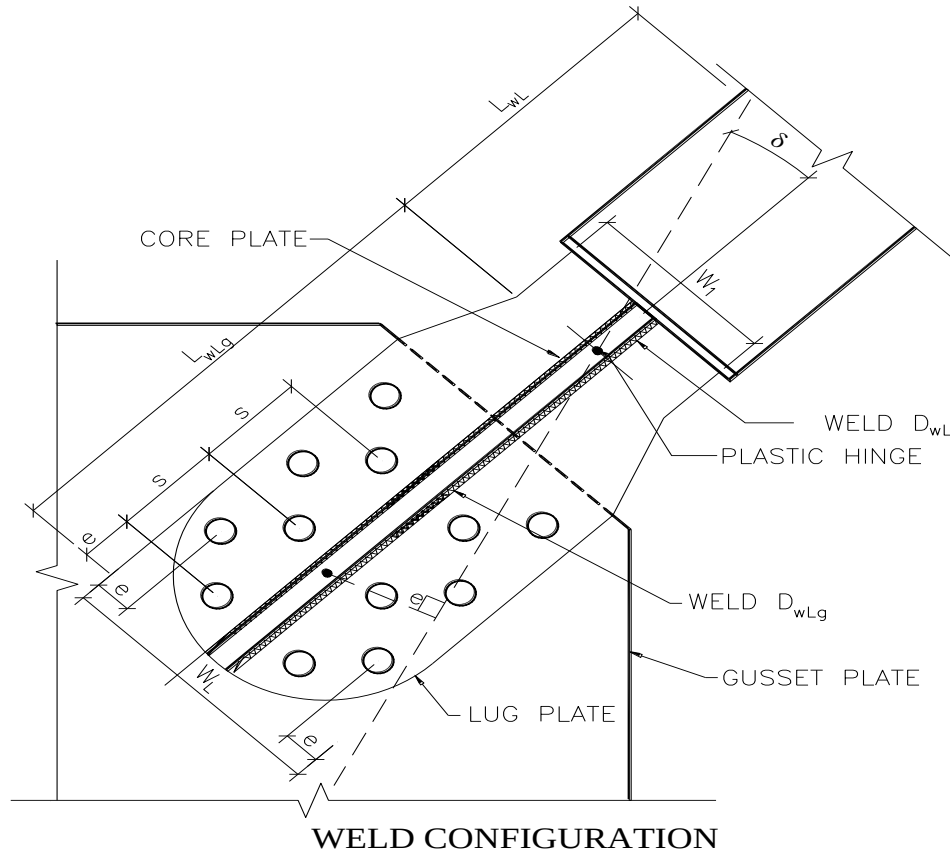
Calculation Submittal Package

Description

Section 3. Brace End Connection Sample Calculation
 End Connection Summary Table

Brace Connection

Example Mark #: 1901
Line 3+, Grid E.5-D.9, Level 2



3.0 DESIGN CRITERIA

Example Mark #: 1901

Compression Strength Adjustment Factor

β : 1.2

Strain Hardening Adjustment Factor

ω : 1.39

Area of (Yielding) Steel Core (as Spec'd on Drawings)
Upper Bound Compressive Yield Stress of Core Material

A_{sc} : 4.00 in² (2581 mm²)
 F_{y-max} : 46 ksi (317 MPa)

Note:

Ry factor not applicable since Fy of core material will be established based on results of coupon tests.

Core Plate Ultimate Tensile Strength
Based on Coupon Test History

F_{usc} : 66 ksi (455 MPa)

Axial Design Load:
Connection Strain Hardening Factor

CF: 1.00

$$P_{ysc-max} = A_{sc} \cdot F_{y-max}$$

$$P_{uT-max} = CF \cdot P_{ysc-max} \cdot \omega$$

$$P_{uC-max} = CF \cdot P_{ysc-max} \cdot \beta \cdot \omega$$

$P_{ysc-max}$:	184.0 kip	(818 kN)
P_{uT-max} :	255.8 kip	(1138 kN)
P_{uC-max} :	306.9 kip	(1365 kN)

Core Dimensions: At Lug Connection	W_t :	4.00 in	(102 mm)
Lug Dimensions: Width of Lug Plate	W_L :	7.50 in	(191 mm)
At Extension Exit from Casing (Transv. Stiffener)	W_i :	4.98 in	(127 mm)
Plate Edge to CL of Bolt	e :	1.63 in	(41 mm)
Bolt Specifications: Number of Bolts in Inside Row	n_i :	3	
Number of Bolts in Outside Row	n_o :	0	
Total Number of Bolts at Each End $2(n_i + n_o)$	n_b :	6	
Bolt Spacing	s :	4.00 in	(102 mm)
Bolt Gage	g :	0.00 in	(0 mm)
Bolt Diameter	d_b :	1.125 in	(29 mm)
Standard Bolt Hole $d_s = d_b + x_{std}$	d_s :	1.250 in	(32 mm)
$x_{std} = 1/8$ " (3.2mm)			
Slip Plane (Single Shear = 1, Double Shear = 2)	n_s :	2	

3.1.0 Bolt Shear - LRFD J3.6

LRFD Resistance Factor

Bolt Shear Strength $F_{nv} = F_{ub} * 0.625 * 0.9 * TCF * CLF$
0.625 = V//T Ratio, 0.9 = Base Connection Length Factor for Non-Uniformity of Loading

Bolt Grade and Ultimate Tensile Strength for Shear **Gr A490/F3148**
 Bolt Thread Condition (N = Include, X = Exclude)
 Thread Condition Factor TCF: IF BTC = "X" then 1.0, IF BTC = "N" then 0.8
 Connection Length Factor Table J3.2 Note b (For $L'_{Lg} > 38"$)
 Connection Length

Bolt Shear Capacity $\phi_r v = \phi_v F_{nv} n_s A_b$
 Bolt Area $A_b = \pi d_b^2 / 4$

Bolt Group Shear Strength $\phi R_v = (n_i + n_o) * 2 * \phi_r v$

Demand-Capacity Ratio

$$DCR_{Shear} = P_{Uc-max} / R_v$$

ϕ_v :	0.75	
F_{nv} :	64.8 ksi	(447 MPa)
F_{ub} :	144 ksi	(993 MPa)
BTC:	N	
TCF:	0.80	
CLF:	1.00	
L'_{Lg} :	8.00 in	(203 mm)
$\phi_r v$:	96.6 kip	(430 kN)
A_b :	0.994 in ²	(641 mm ²)
ϕR_v :	579.7 kip	(2579 kN)

DCR_{Shear} :	0.53
-----------------	------

3.2.0 Bolt Friction - LRFD J3.8

LRFD Resistance Factor for Slip

Min Bolt Tensile Area $A_{Tb_min} = \pi/4 * (d - 0.9743/n)^2$, where n = threads/in

Factor for fillers
 Mean Slip Coefficient
 Bolt Pretension Adjustment Factor, f_t **Gr A490/F3148**
Accounts for fact that some bolt grades, such as F3148, have a specified Tb greater than that associated with Fub alone. If the combined grade A490/F3148 is specified and A490's are used, then Tb would be equal to that for the grade and Fnv would be conservatively low by 1/f_t.

Fastener Tension $T_b = 0.7 * f_t * F_{ub} * A_{Tb_min}$
 Bolt Tension Factor

Bolt Slip Capacity $\phi_r s = \phi_s \mu D_u h_f T_b n_s$

Bolt Group Slip Capacity $\phi R_s = n_b * \phi_r s$

Demand-Capacity Ratio

$$DCR_{Slip} = P_{Ysc-max} / \phi R_s$$

ϕ_s :	0.85	
A_{Tb_min} :	0.763 in ²	(492 mm ²)
h_f :	1.00	
μ :	0.30	
f_t :	1.04	
T_b :	80 kip	(356 kN)
D_u :	1.13	
$\phi_r s$:	46.2 kip	(205 kN)
ϕR_s :	277.1 kip	(1233 kN)

DCR_{Slip} :	0.66
----------------	------

3.3.0 Bearing Strength at Bolt Holes - LRFD J3.10

LRFD Resistance Factor for Bearing or Tearout

3.3.1 Bearing Strength at Gusset Plate

Additional Diameter of Hole in Gusset Plate

Thickness of Gusset Plate:

Thickness of Repad Plate for Design:

Gusset Plate Tensile Strength

Clear Distance Between Edge of Bolt Holes

$$L_{csq} = s - (d_s + ovs_q)$$

Number of Occurances of L_{cs} Per Side

If $n_o = 0$ Then $n_{cs} = n_i - 1$, Otherwise $n_{cs} = n_i - 1/2 + n_o - 1$

ϕ_{brg-v} :	0.75	
ovs_q :	0.19 in	(5 mm)
t_q :	1.00 in	(25 mm)
t_r :	0.00 in	(0 mm)
F_{ug} :	65 ksi	(448 MPa)
L_{csq} :	2.563 in	(65 mm)
n_{cs} :	2.0	

Clear Distance Between Plate Edge and Bolt Hole

$$L_{ceq} = e - (d_s + ovs_d)/2$$

$$L_{ceq}: 0.906 \text{ in} \quad (23 \text{ mm})$$

Number of Occurances of L_{ce} per Side

If $n_o = 0$ Then $n_{ce} = 1$, Otherwise $n_{ce} = 2$

$$n_{ce}: 1.0$$

Clear Distance of Bolt Group $L_{cq} = 2 \cdot (n_{ce} \cdot L_{ceq} + n_{cs} \cdot L_{csq})$

$$L_{cq}: 12.06 \text{ in} \quad (306 \text{ mm})$$

Gusset Plate Bearing Strength at Bolt Holes

$\phi R_{n-brq} = \text{min of:}$

$$\phi_{brq} 1.2 \cdot L_{cg} \cdot (t_g + 2t_r) \cdot F_{ug} = 705.7 \text{ kip} \quad (\text{Clear Dist/Tear-Out Controlled})$$

$$\phi_{brq} 2.4 \cdot d_b \cdot n_b \cdot (t_g + 2t_r) \cdot F_{ug} = 789.8 \text{ kip} \quad (\text{Bearing/Ovalization Controlled})$$

$$\phi R_{n-brq}: 705.7 \text{ kip} \quad (3139 \text{ kN})$$

Bearing Strength Stress Ratio

$$DCR_{brq-g} = P_{uc-max} / \phi_{brq} R_{n-brq}$$

Slip checked at serviceability limit state.

$$DCR_{brq-g}: 0.43$$

3.3.2 Bearing Capacity at Lug Plates

Additional Diameter of Holes in Lug Beyond Standard Hole Diam

$$ovs_l: 0.00 \text{ in} \quad (0 \text{ mm})$$

Lug Plate Thickness

$$t_l: 0.63 \text{ in} \quad (16 \text{ mm})$$

Lug Plate Tensile Strength

$$F_{ul}: 65 \text{ ksi} \quad (448 \text{ MPa})$$

Clear Distance Between Edge of Bolt Holes

$$L_{csl} = s - (d_s + ovs_l)$$

$$L_{csl}: 2.750 \text{ in} \quad (70 \text{ mm})$$

Clear Distance Between Plate Edge and Bolt Hole

$$L_{cel} = e - (d_s + ovs_d)/2$$

$$L_{cel}: 1.000 \text{ in} \quad (25 \text{ mm})$$

Clear Distance of Bolt Group $L_{cl} = 2 \cdot (n_{ce} \cdot L_{cel} + n_{cs} \cdot L_{csl})$

$$L_{cl}: 13.00 \text{ in} \quad (330 \text{ mm})$$

Lug Plate Bearing Strength at Bolt Holes

$\phi R_{n-brq} = \text{min of:}$

$$\phi_{brq} 1.2 \cdot L_{cl} \cdot t_l \cdot F_{ul} \cdot n_s = 950.6 \text{ kip} \quad (4229 \text{ kN}) \quad (\text{Clear Dist/Tear-Out Controlled})$$

$$\phi_{brq} 2.4 \cdot d_b \cdot n_b \cdot t_l \cdot F_{ul} \cdot n_s = 987.2 \text{ kip} \quad (4391 \text{ kN}) \quad (\text{Bearing/Ovalization Controlled})$$

$$\phi R_{n-brq}: 950.6 \text{ kip} \quad (4229 \text{ kN})$$

Bearing Strength Stress Ratio

$$DCR_{brq-l} = P_{uc-max} / \phi_{brq} R_{n-brq}$$

$$DCR_{brq-l}: 0.32$$

3.3.3 Combined Bolt Bearing/Tear-out/Bolt Shear at Lug and Gusset (Bolt by Bolt Method)

Extreme (Edge) Bolts - "Edge Bolts" Use L_{ceg} , "Field Bolts" use L_{csg}

Brace in Tension (T):

Free Edge Bolt when: Lug Field Bolt (LFB) or Gusset Edge Bolt (GEB)

Other Edge Bolt when: Lug Edge Bolt (LEB) or Gusset Edge Bolt (GFB)

Brace in Compression (C):

Free Edge Bolt when: Lug Field Bolt (LFG) or Gusset Edge Bolt (GFB)

Other Edge Bolt when: Lug Field Bolt (LFG) or Gusset Edge Bolt (GFB)

At all Conditions Check Min of Bearing, Edge Tear-out, and Bolt Shear

Gusset

G. Edge Bolts on n_i Row: $\phi_{brq-v} \cdot (t_q + 2t_r) \cdot F_{uq} \cdot \text{MIN}[1.2 \cdot L_{ceg}, 2.4 \cdot d_b]$

$$GEB_{ni}: 53.0 \text{ kip} \quad (236 \text{ kN})$$

G. Edge Bolts on n_o Row: $\phi_{brq-v} \cdot (t_q + 2t_r) \cdot F_{uq} \cdot \text{MIN}[1.2 \cdot (L_{ceg} + 0.5s), 2.4 \cdot d_b]$

$$GEB_{no}: 0.0 \text{ kip} \quad (0 \text{ kN})$$

GEB Capacity = 0 Unless $n_o > 0$

G. Field Bolts on n_i Row: $\phi_{brq-v} \cdot (t_q + 2t_r) \cdot F_{uq} \cdot \text{MIN}[1.2 \cdot L_{csg}, 2.4 \cdot d_b]$

$$GFB_{ni}: 131.6 \text{ kip} \quad (585 \text{ kN})$$

G. Field Bolts on n_o Row: $\phi_{brq-v} \cdot (t_q + 2t_r) \cdot F_{uq} \cdot \text{MIN}[1.2 \cdot (L_{csg} + 0.5s), 2.4 \cdot d_b]$

$$GFB_{no}: 0.0 \text{ kip} \quad (0 \text{ kN})$$

GFB Capacity = 0 Unless $n_o > 0$

Lug

L. Edge Bolts on n_i Row: $\phi_{brq-v} \cdot t_l \cdot F_{ul} \cdot \text{MIN}[1.2 \cdot L_{cel}, 2.4 \cdot d_b] \cdot 2Lugs$

$$LEB_{ni}: 73.1 \text{ kip} \quad (325 \text{ kN})$$

L. Edge Bolts on n_o Row: $\phi_{brq-v} \cdot t_l \cdot F_{ul} \cdot \text{MIN}[1.2 \cdot (L_{cel} + 0.5s), 2.4 \cdot d_b] \cdot 2Lugs$

$$LEB_{no}: 0.0 \text{ kip} \quad (0 \text{ kN})$$

LEB Capacity = 0 Unless $n_o > 0$

L. Field Bolts on n_i Row: $\phi_{brq-v} \cdot t_l \cdot F_{ul} \cdot \text{MIN}[1.2 \cdot L_{csl}, 2.4 \cdot d_b] \cdot 2Lugs$

$$LFB_{ni}: 164.5 \text{ kip} \quad (732 \text{ kN})$$

L. Field Bolts on n_o Row: $\phi_{brq-v} \cdot t_l \cdot F_{ul} \cdot \text{MIN}[1.2 \cdot (L_{csl} + 0.5s), 2.4 \cdot d_b] \cdot 2Lugs$

$$LFB_{no}: 0.0 \text{ kip} \quad (0 \text{ kN})$$

LFB Capacity = 0 Unless $n_o > 0$

Sum of Extreme Bolt Capacities (at each end of each line):

Tension: $2[\text{MIN}(LFB, \phi_{rv} \text{ or } GEB, \phi_{rv}) + \text{MIN}(LEB, \phi_{rv} \text{ or } GFB, \phi_{rv})]$

$$\phi R_{n-TE}: 252.3 \text{ kip} \quad (1122 \text{ kN})$$

Compression: $2[2 \cdot \text{MIN}(LFB, \phi_{rv} \text{ or } GFB, \phi_{rv})]$

$$\phi R_{n-CE}: 386.5 \text{ kip} \quad (1719 \text{ kN})$$

Note Brace in Compression Results in "Field Bolt" Condition for all Extreme Bolts

Sum of Remaining Field Bolt Capacities:

At Gusset: $2[\text{MAX}(n_i - 2, 0) \cdot \text{min}(GFB_{ni}, \phi_{rv}) + \text{MAX}(n_o - 2, 0) \cdot \text{min}(GFB_{no}, \phi_{rv})]$

$$\phi R_{n-GF}: 193.2 \text{ kip} \quad (860 \text{ kN})$$

At Lug: $2[\text{MAX}(n_i - 2, 0) \cdot \text{min}(LFB_{ni}, \phi_{rv}) + \text{MAX}(n_o - 2, 0) \cdot \text{min}(LFB_{no}, \phi_{rv})]$

$$\phi R_{n-LF}: 193.2 \text{ kip} \quad (860 \text{ kN})$$

Total Tension Capacity at Gusset:
Total Compression Capacity at Gusset:
Total Tension Capacity at Lug:
Total Compression Capacity at Lug:

ϕR_{n-TG} : 445.5 kip (1982 kN)
 ϕR_{n-CG} : 579.7 kip (2579 kN)
 ϕR_{n-TL} : 445.5 kip (1982 kN)
 ϕR_{n-CL} : 579.7 kip (2579 kN)

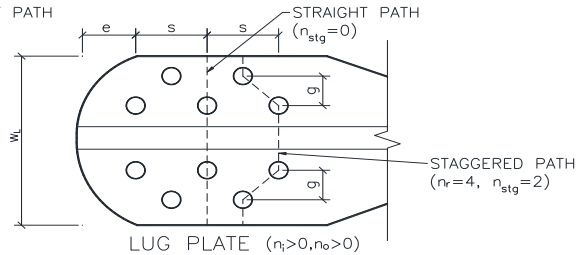
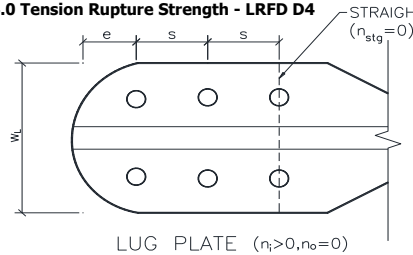
Bearing/Tearout Strength Stress Ratio:

$$DCR_{brg/Tear-G} = \text{MAX}(P_{uc-max}/\phi R_{n-CG}, P_{ut-max}/\phi R_{n-TG})$$

$$DCR_{brg/Tear-L} = \text{MAX}(P_{uc-max}/\phi R_{n-CL}, P_{ut-max}/\phi R_{n-TL})$$

$DCR_{brg/Tear-G}$:	0.57
$DCR_{brg/Tear-L}$:	0.57

3.4.0 Tension Rupture Strength - LRFD D4



LRFD Resistance Factor for Tension Rupture

ϕ_{tr} : 0.75

Thickness of Yielding Core

t_{sc} : 1.00 in (25 mm)

Shear Lag Factor (Table D3.1 Case 2)

U: 0.95

Overslot in Lug for Gusset

OSL_Q : 0.19 in (5 mm)

Net Area Subject to Tension (Use AISC D3 for Staggered Bolt Net Area)

Number of Rows of Bolts If $n_0 = 0$, then $n_r = 2$, otherwise $n_r = 4$

n_r : 2

Stagger Adjustment Term (AISC D4.3b)

If $n_0 = 0$, then $stg = 0$, otherwise $stg = (s/2)^2/(4g)$

stg : 0.00 in (0 mm)

Number of Stagers $n_{stg} = n_r - 2$

n_{stg} : 0

Net Area of Lug Transverse to Line of Force

Staggerd Path: $A_{nTLb1} = 2t_L [W_L - n_r(d_s + ovs_L + 1/16) + n_{stg}stg]$

A_{nTLb1} : 6.09 in² (3931 mm²)

Straight Path: $A_{nTLbx} = 2t_L [W_L - 2(d_s + ovs_L + 1/16)]$

A_{nTLbx} : 6.09 in² (3931 mm²)

$A_{nTLb} = \min(A_{nTLb1}, A_{nTLbx})$

A_{nTLb} : 6.09 in² (3931 mm²)

Net Area of Lug Stiffener

$A_{nTLc} = t_{sc} [W_t - (t_q + 2t_L + OSL_Q)]$

A_{nTLc} : 1.56 in² (1008 mm²)

Lug Plate Tension Rupture Strength

$$\phi R_{n-tr} = \phi_{tr} \cdot U \cdot (F_{ut} \cdot A_{nTLb} + F_{usc} \cdot A_{nTLc})$$

ϕR_{n-tr} : 355.1 kip (1579 kN)

Tension Rupture Stress Ratio

$$DCR_{tr} = P_{ut-max}/\phi R_{n-tr}$$

DCR_{tr} : 0.72

3.5.0 Block Rupture Strength - LRFD J4.3

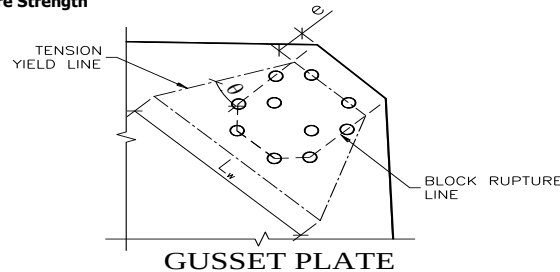
LRFD Resistance Factor

ϕ_{bik} : 0.75

Block Shear Shear-Lag Factor

U_{bs} : 1.00

3.5.1 Gusset Block Rupture Strength



Gusset Plate Yield Strength

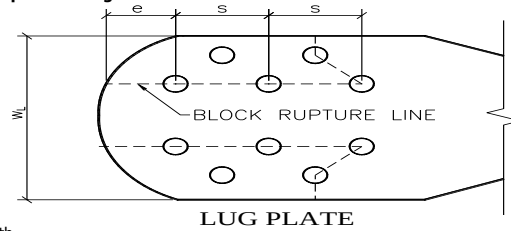
F_{yg} : 50 ksi (345 MPa)

Gusset Plate Edge Distance

e: 1.63 in (41 mm)

Gross Area Subject to Shear				
If	Then	L_{qv-q} :	9.63 in	(244 mm)
$n_o = 0$	$L_{qv-q} = (n_i - 1) \cdot s + e$			
$n_o = n_i$	$L_{qv-q} = (n_o - 1) \cdot s + \sqrt{[(s/2)^2 + g^2]} + e$			
Otherwise	$L_{qv-q} = (n_o - 1/2) \cdot s + \sqrt{[(s/2)^2 + g^2]} + e$			
$A_{qv-q} = 2 \cdot L_{qv-q} \cdot (t_q + 2 \cdot t_r)$		A_{qv-q} :	19.25 in ²	(12419 mm ²)
Net Area Subject to Shear				
Number of Bolt Holes in Shear Path				
If $n_o = 0$, Then $n_{na-q} = n_i - 1/2$, Otherwise $n_{na-q} = n_o + 1/2$		n_{na-q} :	2.5	
Length to be $RL_{nv-q} = (d_s + ovs_q + 1/16) \cdot n_{na-q}$		L_{nv-q} :	3.75 in	(95 mm)
$A_{nv-q} = A_{qv-q} - 2 \cdot L_{nv-q} \cdot (t_q + 2 \cdot t_r)$		A_{nv-q} :	11.75 in ²	(7581 mm ²)
Gross Area Subject to Tension				
$L_{qt-q} = W_L - 2 \cdot (e + g)$		L_{qt-q} :	4.25 in	(108 mm)
Note: $g = 0$ if $n_o = 0$				
$A_{qt-q} = L_{qt-q} \cdot (t_q + 2 \cdot t_r)$		A_{qt-q} :	4.25 in ²	(2742 mm ²)
Net Area Subject to Tension				
$L_{nt-q} = (d_s + ovs_q + 1/16)$		L_{nt-q} :	1.50 in	(38 mm)
$A_{nt-q} = A_{qt-q} - L_{nt-q} \cdot (t_q + 2 \cdot t_r)$		A_{nt-q} :	2.75 in ²	(1774 mm ²)
Gusset Plate Block Rupture Strength				
Shear Rupture Term	$0.6 \cdot F_{uq} \cdot A_{nv-q}$	SRT:	458.3 kip	(2038 kN)
Shear Yield Term	$0.6 \cdot F_{yq} \cdot A_{qv-q}$	SYT:	577.5 kip	(2569 kN)
Tension Rupture Term	$U_{bs} \cdot F_{uq} \cdot A_{nt-q}$	TRT:	178.8 kip	(795 kN)
$\phi R_{n-blk-q} = \phi[\min(SRT, SYT) + TRT]$		$\phi R_{n-blk-q}$:	477.8 kip	(2125 kN)
Block Shear Strength Stress Ratio at Gusset				
$DCR_{blk-g} = P_{ut-max} / \phi R_{n-blk-g}$		DCR_{blk-g} :	0.54	

3.5.2 Lug Plates Block Rupture Strength



Lug Plate Yield Strength		F_{yL} :	50 ksi	(345 MPa)
Gross Area Subject to Shear				
If	Then	L_{qv-L} :	9.63 in	(244 mm)
$n_o = 0$	$L_{qv-L} = (n_i - 1) \cdot s + e$			
Otherwise	$L_{qv-L} = (n_i - 1) \cdot s + \sqrt{[(s/2)^2 + g^2]} + e$			
$A_{qv-L} = 4 \cdot L_{qv-L} \cdot t_L$		A_{qv-L} :	24.06 in ²	(15524 mm ²)
Net Area Subject to Shear				
If $n_o = 0$, Then $n_{na-L} = n_i - 1/2$, Otherwise $n_{na-L} = n_i + 1/2$		n_{na-L} :	2.5	
$L_{nv-L} = (d_s + ovs_L + 1/16) \cdot n_{na-L}$		L_{nv-L} :	3.28 in	(83 mm)
$A_{nv-L} = A_{qv-L} - 4 \cdot L_{nv-L} \cdot t_L$		A_{nv-L} :	15.86 in ²	(10232 mm ²)
Gross Area Subject to Tension				
$A_{qt-L} = 4 \cdot e \cdot t_L$		A_{qt-L} :	4.06 in ²	(2621 mm ²)
Net Area Subject to Tension				
$L_{nt-L} = (d_s + ovs_L + 1/16)/2$		L_{nt-L} :	0.66 in	(17 mm)
$A_{nt-L} = A_{qt-L} - L_{nt-L} \cdot t_L \cdot 4$		A_{nt-L} :	2.42 in ²	(1562 mm ²)
Lug Plate Block Rupture Strength				
Shear Rupture Term	$0.6 \cdot F_{uL} \cdot A_{nv-L}$	SRT:	618.5 kip	(2751 kN)
Shear Yield Term	$0.6 \cdot F_{yL} \cdot A_{qv-L}$	SYT:	721.9 kip	(3211 kN)
Tension Rupture Term	$U_{bs} \cdot F_{uL} \cdot A_{nt-L}$	TRT:	157.4 kip	(700 kN)
$\phi R_{n-blk-L} = \phi[\min(SRT, SYT) + TRT]$		$\phi R_{n-blk-L}$:	582.0 kip	(2589 kN)

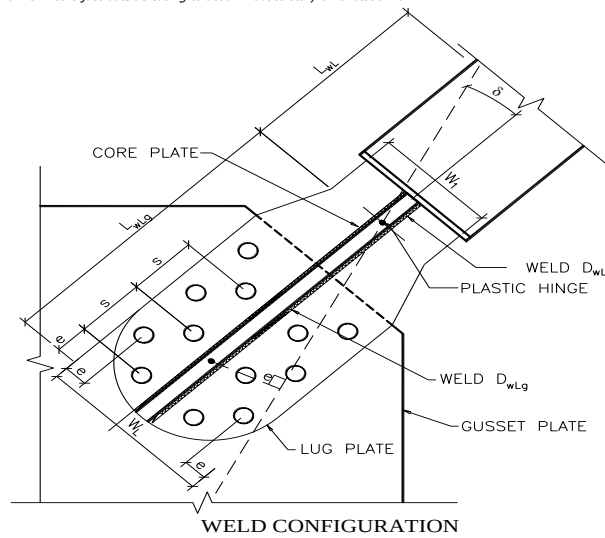
Block Shear Strength Stress Ratio at Lug

$$DCR_{blk-L} = P_{ut-max} / \phi R_{n-blk-L}$$

$$DCR_{blk-L} = 0.44$$

3.6.0 Weld Design

Assume plastic hinge forms in core just outside casing to accommodate story drift rotation δ



LRFD Resistance Factor

$$\phi_{Weld} = 0.75$$

Upper Bound Compressive Yield Stress of Core Material

$$F_{ysc-max} = 46 \text{ ksi} \quad (317 \text{ MPa})$$

Weld Material Minimum Yield Strength for BRB Components

$$F_{exx,BRB} = 70 \text{ ksi} \quad (483 \text{ MPa})$$

Length of Lug to Core Weld at Bolt Pattern

$$L_{wLg} = 15.25 \text{ in} \quad (387 \text{ mm})$$

Length of Lug to Core Weld beyond Bolt Pattern

$$L_{wL} = 25.46 \text{ in} \quad (647 \text{ mm})$$

Weld Both Sides of Lug Beyond Bolt Pattern?

$$WBS = \text{TRUE}$$

Width of Steel Yielding Core

$$W_{sc} = 4.00 \text{ in} \quad (102 \text{ mm})$$

Width of Stiffener at Lug

$$W_s = 0.78 \text{ in} \quad (20 \text{ mm})$$

Thickness of Stiffener at Lug

$$t_s = 1.00 \text{ in} \quad (25 \text{ mm})$$

3.6.1 Weld Size Required at Bolt Pattern

Percent of Core Stub Capacity at Lug Allowed to be Transferred thru that Section (max 100%).

$$\%A_{sc-stub} = 100\%$$

Max Force in Stiffener at Lug

$$P_{wLg} = P_{uc-max} \cdot W_g / W_{sc} \cdot \min(\%A_{sc-stub}, 1.0)$$

*Conservative for sizing weld

$$P_{wLg} = 59.9 \text{ kip} \quad (267 \text{ kN})$$

Min Weld Size Based on Material Thickness

$$\begin{aligned} \text{IF } \min(t_s, t_g) \leq 1/2" & \quad \text{Then } D_{wLg-min} = 3^{16\text{ths}} \\ \min(t_s, t_g) \leq 3/4" & \quad D_{wLg-min} = 4^{16\text{ths}} \\ \text{Otherwise} & \quad D_{wLg-min} = 5^{16\text{ths}} \end{aligned}$$

$$D_{wLg-min} = 4.00 \text{ (16ths)} \quad (6 \text{ mm})$$

Weld Size Based on Required Force

$$D'_{wLg} = P_{wLg} / (\phi_{Weld} \cdot 0.6 \cdot F_{exx} \cdot 0.7071 \cdot 2 \cdot L_{wLg}) \cdot 16$$

$$D'_{wLg} = 1.41 \text{ (16ths)} \quad (2 \text{ mm})$$

Required Weld Size

$$\begin{aligned} D_{wLg} &= 4.00 \quad (6 \text{ mm}) \\ D_{wLg} &= 4.00 \text{ (16ths)} \quad (6 \text{ mm}) \\ D_{wLg} &= 1/4" \quad (6 \text{ mm}) \end{aligned}$$

Base Metal Thickness Check

$$\begin{aligned} t_{min}/t_{s,c} &= \text{Max of:} \\ 1 \cdot F_{EXX,BRB} \cdot 0.7071 \cdot (D_{wLg}/16) / (F_{ul} \cdot t_s) &= 0.305 \\ 2 \cdot F_{EXX,BRB} \cdot 0.7071 \cdot (D_{wLg}/16) / (F_{usc} \cdot t_s) &= 0.375 \end{aligned}$$

$$DCR_{Weld-Lg} = 0.37$$

3.6.2 Weld Size Required Beyond Bolt Pattern

Yield Strength of Stub Section

$$F_{Y-WLQ} = W_s \cdot t_s \cdot F_{YSC-max} \cdot \min(\%A_{SC-Stub}, 1.0)$$

**Conservative for determining force in section before stub*

$$F_{Y-WLQ} = 35.9 \text{ kip} \quad (160 \text{ kN})$$

Force in Weld Beyond Bolt Group

$$P_{WL} = P_{UC-max} \cdot 2 \cdot F_{Y-WLQ}$$

$$P_{WL} = 235.0 \text{ kip} \quad (1045 \text{ kN})$$

Weld Size Based on Required Force

$$D'_{WL} = P_{WL} / (\phi_{Weld} \cdot 0.6 \cdot F_{exx} \cdot 0.7071 \cdot 4 \cdot L_{WL}) \cdot 16$$

$$D'_{WL} = 1.66 \text{ (16ths)} \quad (3 \text{ mm})$$

Required Weld Size

Note that minimum weld size here equal to minimum size req'd at bolt pattern ($D_{WLG-min}$) since lug and core thickness are the same as at that location.

$$D_{WL} = 4.00 \text{ (16ths)} \quad (6 \text{ mm})$$

$$D_{WL} = 4.00 \text{ (16ths)} \quad (6 \text{ mm})$$

$$D_{WL} = 1/4 \text{ " } \quad (6 \text{ mm})$$

Base Metal Thickness Check

Factor for Weld Both Sides (WBS) Beyond Bolt Pattern:

IF WBS = TRUE Then WBSF = 2, Otherwise WBSF = 1

$$WBSF = 2$$

$t_{min}/t_{LSC} = \text{Max of:}$

$$WBSF \cdot F_{EXX,BRB} \cdot 0.7071 \cdot (D_{WL}/16) / (F_{UL} \cdot t_L) = 0.609$$

$$2 \cdot F_{EXX,BRB} \cdot 0.7071 \cdot (D_{WL}/16) / (F_{USC} \cdot t_{SC}) = 0.375$$

$$DCR_{Weld-L} = 0.61$$

3.6.3 Weld Around Lug in Lieu of Bolting

Weld Material Minimum Yield Strength for Lug to Gusset (Alt Weld)

$$F_{exx,Gst} = 70 \text{ ksi} \quad (483 \text{ MPa})$$

Length of Sides of Lug Only

$$L_{LS} = (L_{LG} - W_L/2 - Tol_{LLS}) \cdot 4$$

$$Tol_{LLS} = 0.50 \text{ in} \quad (13 \text{ mm})$$

Length Around Lug (Including Sides)

$$L_{LRS} = L_{LS} + \pi \cdot (W_L/2) \cdot 2$$

$$L_{LS} = 32.54 \text{ in} \quad (826 \text{ mm})$$

$$L_{RS} = 56.10 \text{ in} \quad (1425 \text{ mm})$$

Plastic Section Modulus of Core Extension (Section Just Outside Casing)

$$Z_+ = (2t_L \cdot W_L^2 + (W_L - 2t_L) \cdot t_{SC}^2) / 4$$

$$Z_+ = 8.44 \text{ in}^3 \quad (138371 \text{ mm}^3)$$

Force Couple to Resist Plastification of Core Extension $F_R = Z_+ \cdot F_{YL} / W_L$

$$F_R = 56.3 \text{ kip} \quad (250 \text{ kN})$$

Required Weld if Welded Around Lug

$$D_{RS} = (P_{UC-max} + 2 \cdot F_R) / (L_{RS} \cdot 0.7071 \cdot 0.6 \cdot \phi_{Weld} \cdot F_{exx,Gst}) \cdot 16$$

$$D_{RS} = 5.37 \quad (9 \text{ mm})$$

$$D_{RS} = 6.00 \text{ (16ths)} \quad (10 \text{ mm})$$

$$D_{RS} = 3/8 \text{ " } \quad (10 \text{ mm})$$

Required Weld if Welded Around Sides of Lug Only

$$D_S = (P_{UC-max} + 2 \cdot F_R) / (L_{LS} \cdot 0.7071 \cdot 0.6 \cdot \phi_{Weld} \cdot F_{exx,Gst}) \cdot 16$$

$$D_S = 9.26 \quad (15 \text{ mm})$$

$$D_S = 10.00 \text{ (16ths)} \quad (16 \text{ mm})$$

$$D_S = 5/8 \text{ " } \quad (16 \text{ mm})$$

3.7.0 Summary

3.1.0 Bolt Shear

$$DCR_{Shear} = 0.53$$

3.2.0 Bolt Friction

$$DCR_{Slip} = 0.66$$

3.3.1 Bolt Bearing - Gusset Plate

$$DCR_{brq-g} = 0.43$$

3.3.2 Bolt Bearing - Lug Plates

$$DCR_{brq-L} = 0.32$$

3.3.3 Combined Bolt Bearing & Tearout - Gusset

$$DCR_{bra/Tear-G} = 0.57$$

3.3.3 Combined Bolt Bearing & Tearout - Lug

$$DCR_{bra/Tear-L} = 0.57$$

3.4.0 Tension Fracture - Lug Plates

$$DCR_{tr} = 0.72$$

3.5.1 Block Rupture - Gusset Plate

$$DCR_{blk-g} = 0.54$$

3.5.2 Block Rupture - Lug Plates

$$DCR_{blk-L} = 0.44$$

3.6.1 Weld Strength at Bolt Pattern

$$DCR_{Weld-Lq} = 0.37$$

3.6.2 Weld Strength Beyond Bolt Pattern

$$DCR_{Weld-L} = 0.61$$

$$\text{Max: } 0.72$$

END CONNECTION CALCULATIONS

Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

Specimen ID and Location						Section 3.0 Design Criteria																			Section 3.1.0 Bolt Shear - LRFD J3.6										Section 3.2.0 Bolt Friction - LRFD J3.8												
EOR-ID #	Line	Grids #	Lvls #	Mark #	Qty #	β	ω	A_{sc} in ²	$F_{y,max}$ ksi	$F_{u,sc}$ ksi	CF	$P_{ysc,max}$ kip	$P_{uT,max}$ kip	$P_{uC,max}$ kip	W_T in	W_L in	W_1 in	e in	n_l	n_o	n_b	s in	g in	d_b in	d_s in	n_s	ϕ_v	F_{nv} ksi	$F_{u,bolt}$ ksi	BTC	TCF	CLF	L'_{Lg} in	ϕ_{rv} kip	A_b in ²	ϕ_{R_v} kip	DCR_{Shear}	ϕ_s	$A_{Tb,min}$ in ²	h_f	μ	f_T	T_b kip	D_u	ϕ_{fs} kip	ϕ_{R_s} kip	DCR_{Slip}
BRB-4.00	3+	E.5-D.9	2	1901	1	1.20	1.39	4.00	46	66	1.0	184	256	307	4.000	7.50	4.98	1.625	3	0	6	4.000	0.000	1.125	1.25	2	0.75	64.8	144	N	0.80	1.00	8.0	96.6	0.994	580	0.53	0.85	0.76	1.00	0.30	1.04	80	1.13	46	277	1.11
BRB-4.00	3+	E.5-D.9	1	1902	1	1.19	1.38	4.00	46	66	1.0	184	254	302	4.000	7.50	4.90	1.625	3	0	6	4.000	0.000	1.125	1.25	2	0.75	64.8	144	N	0.80	1.00	8.0	96.6	0.994	580	0.52	0.85	0.76	1.00	0.30	1.04	80	1.13	46	277	1.09

END CONNECTION CALCULATIONS

Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

Specimen ID and Location						Section 3.3.0 Bearing Strength at Bolt Holes - LRFD J3.10																																								
						Gen	Section 3.3.1 Bearing Strength at Gusset Plate								Section 3.3.2 Bearing Capacity at Lug Plates								Section 3.3.3 Combined Bolt Bearing/ Tear-out/ Bolt Shear at Lug and Gusset (Bolt by Bolt Method)																							
EOR-ID	Line	Grids	Lvls	Mark	Qty	ϕ_{brg-V}	ϕS_g	t_g	$t_{r,Des}$	F_{ug}	L_{cs}	n_{cs}	L_{ce}	n_{ce}	L_{cg}	ϕR_{n-brg}	DCR_{brg-g}	ϕS_L	t_L	F_{uL}	L_{csL}	L_{ceL}	L_{cL}	ϕR_{n-brg}	DCR_{brg-L}	GEB_{nl}	GEB_{no}	GFB_{nl}	GFB_{no}	LEB_{nl}	LEB_{no}	LFB_{nl}	LFB_{no}	$\phi R_{n-T,Edge}$	$\phi R_{n-C,Edge}$	$\phi R_{n-G,Field}$	$\phi R_{n-L,Field}$	ϕR_{n-TG}	ϕR_{n-CG}	ϕR_{n-TL}	ϕR_{n-CL}	P_u	P_u			
#		#	#	#	#		in	in	in	ksi	in		in		in	kip		in	in	ksi	in	in	in	in	kip		kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip	kip
BRB-4.00	3+	E.5-D.9	2	1901	1	0.75	0.19	1.00	0.000	65	2.56	2.00	0.91	1.00	12.1	706	0.43	0.000	0.63	65	2.75	1.00	13.0	951	0.32	53	0	132	0	73	0	165	0	252	386	193	193	446	580	446	580	0.57	0.57			
BRB-4.00	3+	E.5-D.9	1	1902	1	0.75	0.19	1.00	0.000	65	2.56	2.00	0.91	1.00	12.1	706	0.43	0.000	0.63	65	2.75	1.00	13.0	951	0.32	53	0	132	0	73	0	165	0	252	386	193	193	446	580	446	580	0.57	0.57			



END CONNECTION CALCULATIONS

Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

Specimen ID and Location						Section 3.4.0 Tension Rupture Strength - LRFD D4														Section 3.5.0 Block Rupture Strength - LRFD J4.3																													
																				General		Section 3.5.1 Gusset Block Rupture Strength														Section 3.5.2 Lug Plates Block Rupture Strength													
EOR-ID	Line	Grids	Lvls	Mark	Qty	ϕ_{tr}	t_{sc}	U	OSL_g	n_r	stg	n_{stg}	A_{ntLb1}	A_{ntLbx}	A_{ntLb}	A_{ntLc}	ΦR_{n-tr}	DCR _{tr}	ϕ_{blk}	U_{bs}	F_y	L_{gv-g}	$A_{gv,g}$	n_{na-g}	L_{nv-g}	$A_{nv,g}$	L_{gt-g}	$A_{gt,g}$	L_{nt-g}	$A_{nt,g}$	SRT	SYT	TRT	$\Phi R_{n,g}$	P_u	F_{yL}	L_{gv-L}	$A_{gv,L}$	n_{na-L}	L_{nv-L}	$A_{nv,L}$	$A_{gt,L}$	L_{nt-L}	$A_{nt,L}$	SRT	SYT	TRT	$\Phi R_{n,L}$	P_u
#		#	#	#	#		in		in		in		in ²	in ²	in ²	in ²	kip				ksi	in	in ²			in	in ²	in	in ²	in	in ²	kip	kip	kip	kip		ksi	in	in ²		in	in ²	in	in ²	kip	kip	kip	kip	
BRB-4.00	3+	E.5-D.9	2	1901	1	0.75	1.000	0.95	0.19	2	0.00	0	6.09	6.09	6.09	1.56	355	0.72	0.75	1.0	50	9.6	19.3	2.5	3.75	11.8	4.3	4.3	1.5	2.8	458	578	179	478	0.54	50	9.6	24.1	2.5	3.28	15.9	4.1	0.7	2.4	619	722	157	582	0.44
BRB-4.00	3+	E.5-D.9	1	1902	1	0.75	1.000	0.95	0.19	2	0.00	0	6.09	6.09	6.09	1.56	355	0.72	0.75	1.0	50	9.6	19.3	2.5	3.75	11.8	4.3	4.3	1.5	2.8	458	578	179	478	0.53	50	9.6	24.1	2.5	3.28	15.9	4.1	0.7	2.4	619	722	157	582	0.44

END CONNECTION CALCULATIONS

Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

Specimen ID and Location						Section 3.6.0 Weld Design																											
						Weld Design Criteria								Section 3.6.1 Weld Size Required at Bolt Pattern						3.6.2 Weld Size Beyond Pattern					3.6.3 Weld Around Lug in Lieu of Bolting								
EOR-ID	Line	Grids	Lvls	Mark	Qty	ϕ_{Weld}	F_{sc-max} ksi	$F_{exx,BRB}$ ksi	L_{wLg} in	L_{wL} in	Weld 2 Sides?	W_{sc} in	W_s in	t_s in	$\%A_{sc-stub}$	P_{wLg} kip	D_{wL-min} 16ths	$D_{wLg-req'd}$ 16ths	D_{wLg} 16ths	$\bar{t}_{min}$ $t_{g,sc}$	F_{Y-wLg} kip	P_{wL} kip	$D_{wL-req'd}$ 16ths	D_{wL} 16ths	$\bar{t}_{min}$ $t_{g,sc}$	$F_{exx,Gst}$ ksi	L_{Ls} in	L_{L+g} in	Z in³	F_R kip	D_{rs} 16ths	D_s 16ths	
#		#	#	#	#																												
BRB-4.00	3+	E.5-D.9	2	1901	1	0.75	46	70	15	25	TRUE	4.00	0.78	1.00	100%	60	4.0	1.4	4	0.37	36	235	1.7	4	0.61	70	33	56	8.4	56	6.0	10.0	
BRB-4.00	3+	E.5-D.9	1	1902	1	0.75	46	70	15	25	TRUE	4.00	0.78	1.00	100%	59	4.0	1.4	4	0.37	36	230	1.6	4	0.61	70	33	56	8.2	55	6.0	10.0	

Reed College Central Plant Upgrade

Calculation Submittal Package

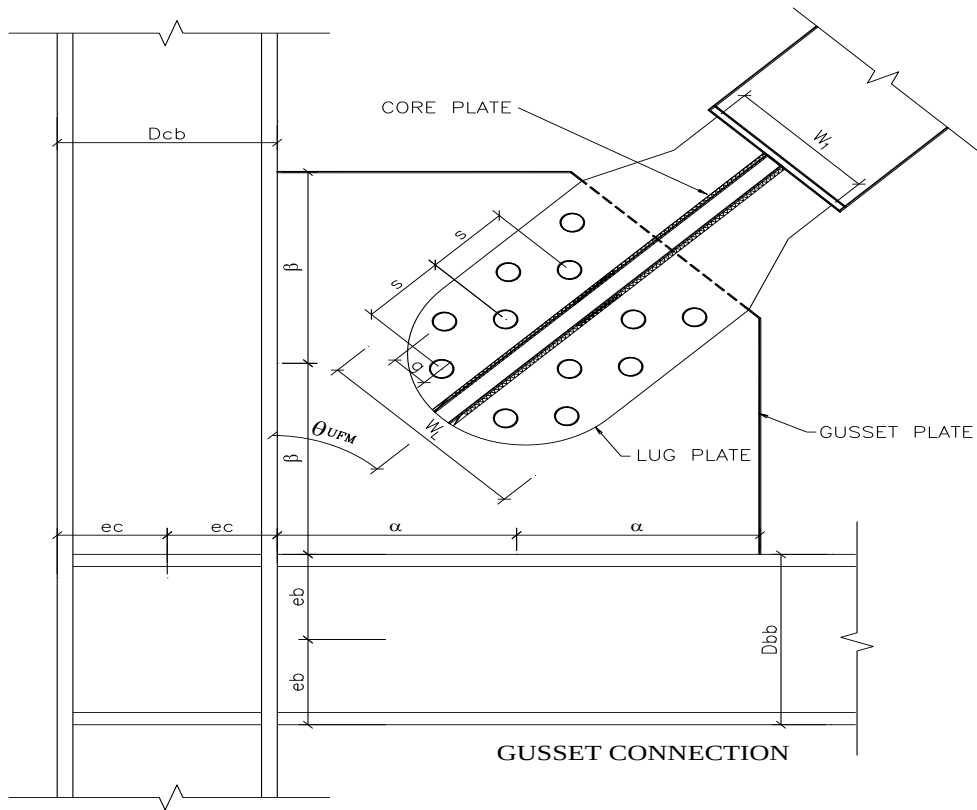
Description

Section 4. Bottom Gusset Beam to Column Flange (Strong-Axis) Connection Sample Calculation
Top and Bottom Connection Summary Tables

Bottom Gusset Connection

(Top Connection Similar)

Example Mark #: 1901
Line 3+, Grid E.5-D.9, Level 2



Uniform Force Method - AISC 360 - Bracing Section**4.0 DESIGN CRITERIA**

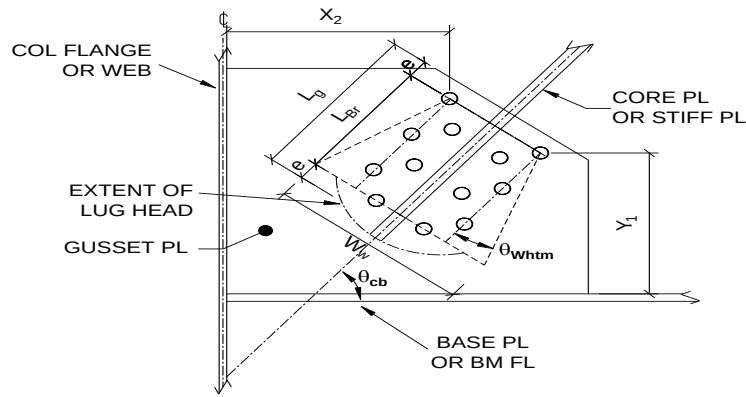
Area of Yielding Steel Core	A_{sc} :	4.00 in ²	(2581 mm ²)
Maximum Yield Stress of Core Material	F_{y-max} :	46 ksi	(317 MPa)
Compression Strength Adjustment Factor	β :	1.2	
Strain Hardening Adjustment Factor	ω :	1.39	
Connection Strain Hardening Factor	CF:	1.00	
Adjusted Brace Strength (Design Axial Load) in Compression ($CF \cdot \beta \omega F_{y-max} A_{sc}$)	P_{uc} :	306.9 kip	(1365 kN)
Adjusted Brace Strength (Design Axial Load) in Tension ($CF \cdot \omega F_{y-max} A_{sc}$)	P_{ut} :	255.8 kip	(1138 kN)
Width of Lug	W_L :	7.50 in	(191 mm)
Column Depth	D_{cb} :	8.00 in	(203 mm)
Column Web Thickness	t_{wc} :	0.75 in	(19 mm)
Column Flange Thickness	t_{fc} :	0.38 in	(10 mm)
Column Flange Width	b_{fc} :	8.00 in	(203 mm)
Column Web Doubler Plate Thickness (one side)	t_{wCPL} :	0.00 in	(0 mm)
Beam Depth	D_{bb} :	8.00 in	(203 mm)
Nominal Depth of Beam	DN_{bb} :	8.00 in	(203 mm)
Beam Web Thickness	t_{wb} :	0.75 in	(19 mm)
Beam Flange Thickness	t_{fb} :	0.38 in	(10 mm)
Beam Flange Width	b_{fb} :	8.00 in	(203 mm)
Beam Distance from Outer Face of Flange to Toe of Fillet	k_{desb} :	1.00 in	(25 mm)
Column Distance from Outer Face of Flange to Toe of Fillet	k_{desc} :	1.00 in	(25 mm)
Beam Web Doubler Plate Thickness (one side)	t_{wBPL} :	0.00 in	(0 mm)
Angle Between the Beam and Brace CL	θ_{CB} :	0.946 rad	54.2°
Angle Between the Column and Brace CL	θ_{UFM} :	0.625 rad	35.8°
Min Clear Distance from Face of Beam to Edge of Lug	b_{bot-Bm} :	1.00 in	(25 mm)
Min Clear Distance from Face of Column to Edge of Lug	$b_{bot-Col}$:	1.17 in	(30 mm)
Gusset Extension to Beam	Ext_B :	1.00 in	(25 mm)
Gusset Extension to Column	Ext_C :	0.75 in	(19 mm)
Distance from Last Bolt to Start of Radius on Lug	b_r :	0.99 in	(25 mm)
Bolt Edge Distance	e :	1.63 in	(41 mm)
Provided Stroke Distance at Each End of Brace	c :	3.00 in	(76 mm)
Distance Between End of Core and Gusset	a :	4.00 in	(102 mm)

4.1.0 GEOMETRY CALCULATIONS - UNIFORM FORCE METHOD

Length from WP to Bottom Tip of Brace			
Length from WP to Outside Edge of Col along WorkLine			
$L_{cb} = (D_{cb}/2)/\cos(\theta_{CB})$	L_{cb} :	6.84 in	(174 mm)
Length from Edge of Column to Tip of CB along WL			
$L_{1cb} = [b_{bot-Col} + (W_L/2)]/\cos(\theta_{CB}) - (e + b_r)$	L_{1cb} :	5.79 in	(147 mm)
Length from WP to Top Edge of Beam along WL			
$L_{bb} = (DN_{bb}/2)/\sin(\theta_{CB})$	L_{bb} :	4.93 in	(125 mm)
Length from Edge of Beam to Tip of CB along WL			
$L_{1bb} = [b_{bot-Bm} + (W_L/2)]/\sin(\theta_{CB}) - (e + b_r)$	L_{1bb} :	3.24 in	(82 mm)
Controlling Length is MAX($L_{cb} + L_{1cb}$, $L_{bb} + L_{1bb}$)	L_{tb} :	12.63 in	(321 mm)

Length from Square Projection to Edge of Gusset (CB Lap on Gusset)	L_g :	11.25 in	(286 mm)
Horizontal Distance from Column to WP ($D_{cb}/2$)	e_c :	4.00 in	(102 mm)
Vertical Distance from Beam to WP ($DN_{bb}/2$)	e_b :	4.00 in	(102 mm)
Minimum Weld on Column from Geometry $L_{gc_min} = (L_{tb} + L_g) \cdot \sin(\theta_{cb}) + (W_l/2 + Ext_c) \cdot \cos(\theta_{cb}) - DN_{bb}/2$	L_{gc_min} :	17.99 in	(457 mm)
Minimum Weld on Beam from Geometry $L_{gb_min} = (L_{tb} + L_g) \cdot \cos(\theta_{cb}) + (W_l/2 + Ext_b) \cdot \sin(\theta_{cb}) - D_{cb}/2$	L_{gb_min} :	13.82 in	(351 mm)
Dist from Face of Col Fl to Centroid of Gusset-to-Beam Connection (UFM) $\alpha_{min} = L_{gb_min}/2$	α_{min}	6.91 in	(176 mm)
$\alpha_{Hand} = \text{Hand Input Value to Force}$	α_{Hand}	6.91 in	(176 mm)
If Hand Input Value is Different from α_{min} use Hand Input Value	α_{min} :	6.91 in	(176 mm)
Inside Weld Deducts:	$WD_{Bm,In}$:	1.50 in	(38 mm)
Outside Weld Deducts:	$WD_{Bm,Out}$:	0.50 in	(13 mm)
α Dist for Weld (1/2 of the actual weld length used for design)	α_q :	5.91 in	(150 mm)
α Dist from face of column to mid point on beam welds $\alpha_{bar} = WD_{Bm,In} + \alpha_q$	α_{bar} :	7.41 in	(188 mm)
Dist from Face of Beam Fl to Centroid of Gusset-to-Column Connection (UFM) $\beta_{min} = L_{gc_min}/2$	β_{min}	9.00 in	(229 mm)
$\beta_{Hand} = \text{Hand Input Value to Force}$	β_{Hand}	9.00 in	(229 mm)
If Hand Input Value is Different from β_{min} use Hand Input Value	β_{min} :	9.00 in	(229 mm)
Inside Weld Deducts:	$WD_{Col,In}$:	1.50 in	(38 mm)
Outside Weld Deducts:	$WD_{Col,Out}$:	0.50 in	(13 mm)
β Dist for Weld (1/2 of the actual weld length used for design)	β_q :	8.00 in	(203 mm)
β from face of beam to mid point on column welds $\beta_{bar} = WD_{Col,In} + \beta_q$	β_{bar} :	9.50 in	(241 mm)
Constants for Connections not in Equilibrium $K = e_b \tan(\theta_{UFM}) - e_c$	K:	-1.11 in	(-28 mm)
$K' = \alpha_{bar} L [\tan(\theta_{UFM}) + \alpha_{bar}/\beta_{bar}]$	K':	11.13 in	(283 mm)
$D = (\tan(\theta_{UFM}))^2 + (\alpha_{bar}/\beta_{bar})^2$	D:	1.13	
Final values of α and β $\alpha_{nE} = [K' \cdot \tan(\theta_{UFM}) + K(\alpha_{bar}/\beta_{bar})^2]/D$	α_{nE} :	6.51 in	(165 mm)
$\beta_{nE} = [K' - K \cdot \tan(\theta_{UFM})]/D$	β_{nE} :	10.56 in	(268 mm)
$r = \sqrt{(\alpha_{nE} + e_c)^2 + (\beta_{nE} + e_b)^2}$	r:	17.96 in	(456 mm)

4.2.0 GUSSET STRESS CALCULATIONS - AISC 360



4.2.1 WHITMORE SECTION STRESS CHECK

LRFD Resistance Factor

ϕ_W : 0.90

Number of Bolts in Inside Row

n_i : 3

Number of Bolts in Outside Row

n_o : 0

Total Number of Bolts at Each End $2(n_i + n_o)$

n_b : 6

Bolt Spacing

s : 4.00 in (102 mm)

Minimum Yield Strength of Gusset

F_{yq} : 50 ksi (345 MPa)

Minimum Tensile Strength of Gusset

F_{uq} : 65 ksi (448 MPa)

Thickness of Gusset Plate

t_q : 1.00 in (25 mm)

Thickness of Repad Plate for Design:

t_r : 0.00 in (0 mm)

Whitmore Angle

θ_{Whitm} : 30.0° 0.524 rad

Total Length Between Outer Bolt Holes $L_{br} = L_q - 2e$

L_{br} : 8.00 in (203 mm)

Vertical Distance to Top Bolt on Beam Side of CL

$$Y_1 = L_{gc-min} - (W_L + Ext_c - e) \cdot \cos(\theta_{cb}) - e \cdot \sin(\theta_{cb})$$

Y_1 : 12.80 in (325 mm)

Horizontal Distance to Top Bolt on Column Side of CL

$$X_2 = L_{qb-min} - (W_L + Ext_b - e) \cdot \sin(\theta_{cb}) - e \cdot \cos(\theta_{cb})$$

X_2 : 7.30 in (185 mm)

Whitmore Length if Not Limited by Beam or Column

$$h_{br} = L_{br} / \cos(\theta_{Whitm})$$

h_{br} : 9.24 in (235 mm)

Gusset Condition:

FHG - Full Height Gusset

NFG - Non Full Height Gusset

FHG: FALSE

Whitmore Length if Limited by Beam

IF

Then

FHG = TRUE

$$h_{bm} = h_{br}$$

FHG = FALSE

$$h_{bm} = Y_1 / \sin(\theta_{cb} + \theta_{Whitm})$$

h_{bm} : 12.86 in (327 mm)

Whitmore Length if Limited by Column

$$h_{col} = X_2 / \cos(\theta_{cb} - \theta_{Whitm})$$

h_{col} : 8.00 in (203 mm)

Constrain Whitmore Section within Gusset Plate?

WSG: FALSE

Whitmore Area

IF

Then

WSG = TRUE

$$A_w = [2 \cdot \min(h_{br}, h_{bm}, h_{col}) \cdot \sin(\theta_{Whitm})] \cdot t_q + (W_L - 2e) \cdot (t_q + 2t_r)$$

WSG = FALSE

$$A_w = [2 \cdot L_{br} \cdot \tan(\theta_{Whitm})] \cdot t_q + (W_L - 2e) \cdot (t_q + 2t_r)$$

A_w = 13.49 in² (8702 mm²)

Whitmore Capacity $\phi R_{n-W} = \phi_W \cdot A_w \cdot F_{yq}$

ϕR_{n-W} : 606.9 kip (2700 kN)

Whitmore Stress Ratio

$$DCR_W = P_{ud} / \phi R_{n-W}$$

DCR_W : 0.42

4.2.2 Gusset Plate Buckling

LRFD Resistance Factor for Compression	ϕ_c :	0.90	
Modulus of Elasticity of Gusset Plate Material	E_{gst} :	29000 ksi	(199955 MPa)
Effective Length Factor for Gusset Buckling	K_{qb} :	1.00	
Average Buckling Length <i>Average of L_1, L_2, & L_3. If average is less than zero, zero is used (Gusset is Elastic).</i>	L' :	3.31 in	(84 mm)
Radius of Gyration of Gusset $r_g = \sqrt{(t_g^2/12)}$	r_g :	0.29 in	(7 mm)
Gusset Slenderness Parameter $\lambda = K_{qb} \cdot L' / (r_g \cdot \pi) \cdot \sqrt{(F_{yg}/E_{gst})}$	λ :	0.15	
Gusset Buckling Capacity $\phi R_{n-gb} = \phi_c \cdot 0.658 \cdot (\lambda_c^2) \cdot F_{yg} \cdot A_w$	ϕR_{n-gb} :	601.1 kip	(2674 kN)
Gusset Buckling Capacity Ratio $DCR_{gb} = P_u / \phi R_{n-gb}$	DCR_{gb} :	0.51	

4.2.3 Gusset Plate Buckling (Out-of-Plane)

LRFD Resistance Factor for Bending	ϕ_b :	0.90	
A. Consider Self Weight of Brace Out-of-Plane Acting on Gusset			
Assumed Spectral Acceleration	S_A :	1.00 g	
Factor on S_A	F_{SA} :	0.40	
Importance Factor	I_p :	1.00	
Brace Weight	W_{br} :	0.86 kip	(3.8 kN)
Additional Out-of-Plane Force on Gusset (when present).	$F_{Add1-OOP/End}$:	0.00 kip	(0.0 kN)
Out of Plane Force at Each End of Brace due to BRB Self Weight $SW F_{OOP} = F_{SA} \cdot S_A \cdot I_p \cdot W_{br} / 2 + F_{Add1-OOP/End}$	F_{OOP} :	0.173 kip	(1 kN)
Moment Arm $M_{Arm_OOP} = L_g + a + 2 \cdot C$	M_{Arm_OOP} :	21.25 in	(540 mm)
Resulting Self Weight Out-of-Plane Moment $SW M_{OOP} = F_{OOP} \cdot M_{Arm_OOP}$	M_{OOP} :	3.7 kip-in	(415 kN-mm)
B. Consider Adjusted Brace Strength at Out Of Plane Frame Deformation			
Story Drift Factor (Usually $2x$, But if considering 100% of ABS, Use only 1/3 of this)	F_{SD} :	0.67	
Story Drift (See Stiffness Section for Calculation)	SD :	1.00%	
Drift Angle $\theta_{SD} = \text{ATAN}(SD \cdot F_{SD})$	θ_{SD} :	0.0067	(0.38°)
Percentage of Adjusted Brace Strength to Consider <i>Use either 100% ABS and 1/3 of $2xSD$, or 30% ABS and $2xSD$</i>	F_{ABS} :	100%	
Out of Plane component of $F_{ABS} \times$ Adjusted Brace Strength $P_H = F_{ABS} \cdot P_{uc} \cdot \text{SIN}(\theta_{SD})$	P_H :	2.05 kip	(9.1 kN)
Moment Arm (consider PH applied at centroid of BRB-gusset connection) $M_{Arm_PH} = L_{Lg} / 2$	M_{Arm_PH} :	5.63 in	(143 mm)
Resulting Horizontal Moment $M_{PH} = P_H \cdot M_{Arm_PH}$	M_{PH} :	11.51 k-in	(1301 kN-mm)

C. Consider Total Moment from Part A and B

Total Out of Plane Moment

$$M_u = M_{OOP} + M_{PH}$$

$$M_u: 15 \text{ k-in} \quad (1716 \text{ kN-mm})$$

Length of potential yielding line (disregarding concrete where occurs)

To Intersection with Column

$$L_c: 13.0 \text{ in} \quad (329 \text{ mm})$$

To Intersection with Beam/BP

$$L_b: 12.3 \text{ in} \quad (313 \text{ mm})$$

Total Length $L_t = L_c + L_b$

$$L_t: 25.3 \text{ in} \quad (642 \text{ mm})$$

Plastic Modulus

$$Z_p = L_t \cdot t_g^2 / 4$$

$$Z_p: 6.32 \text{ in}^3 \quad (103536 \text{ mm}^3)$$

Design Flexural Strength

$$\phi M_n = \phi_b \cdot Z_p \cdot F_y$$

$$\phi M_n: 284 \text{ k-in} \quad (32128 \text{ kN-mm})$$

Gusset Flexure Capacity Ratio

$$DCR_{gf} = M_u / \phi M_n$$

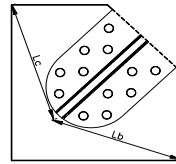
$DCR_{gf}:$	0.05
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Combined Gusset Buckling & Flexure DCR

$$\text{IF } DCR_{gb} \geq 0.2, \quad DCR_{gb+f} = DCR_{gb} + (8/9)DCR_{gf}$$

$$\text{IF } DCR_{gb} < 0.2, \quad DCR_{gb+f} = (1/2)DCR_{gb} + DCR_{gf}$$

$DCR_{gb+f}:$	0.56
$DCR_{gb+f}:$	-



4.8.0 Summary

4.2.1 Whitmore Section Stress	DCR_{Wf}	0.42
4.2.2 Gusset Plate Buckling	DCR_{qb}	0.51
4.2.3 Gusset Plate Combined Buckling & Flexure	DCR_{qb+fb}	0.56
4.4.2 Column Web Shear Check	DCR_{cwv}	n.a.
4.6.1A Gusset Weld Base Metal Check at Beam (Gusset)	DCR_{wbmbq}	n.a.
Gusset Weld Base Metal Check at Beam (Flange)	DCR_{wbmbf}	n.a.
4.6.1B Gusset Weld Base Metal Check at Column (Gusset)	DCR_{wbmcg}	n.a.
Gusset Weld Base Metal Check at Column (Flange)	DCR_{wbmcf}	n.a.
4.6.1C Beam Weld Filler Material Base Metal Compatability Check	$DCR_{wbm,8m}$	n.a.
Column Weld Filler Material Base Metal Compatability Check	$DCR_{wbm,Col}$	n.a.
4.7.1 Beam Web Yield Check	DCR_{wyb}	n.a.
4.7.1 Column Web Yield Check	DCR_{wyc}	n.a.
4.7.2 Beam Web Crippling Check	DCR_{wcb}	n.a.
4.7.2 Column Web Crippling Check	DCR_{wcc}	n.a.
<i>Provide Stiffener if DCR_{wyb} or $DCR_{wcb} > 1.0$</i>		

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EOR-ID #	Line	Grids #	Lvls #	Mark #	Qty #	A _{sc} in ²	F _y -max ksi	β	ω	CF	P _{uc} kip	P _{ut} kip	W _L in	D _{cb} in	t _{wc} in	t _{fc} in	b _{fc} in	t _{wc} PL in	D _{db} in	D _{Ndb} in	t _{wb} in	t _{fb} in	b _{fb} in	k _{desb} in	k _{desc} in	t _{wbb} PL in	θ _{CB} rad	θ _{UFM} rad	b _{bot-Bm} in	b _{bot-Col} in	Ext _b in	Ext _c in	b _r in	e in	c in	a in
BRB-4.00	3+	E-5-D.9	2	1901	1	4.00	46	1.20	1.39	1.00	307	256	7.50	8.0	0.75	0.38	8.00	0.00	8.0	8.0	0.75	0.38	8.00	1.00	1.00	0.00	0.95	0.63	1.00	1.17	1.00	0.75	0.99	1.63	3.0	4.0
BRB-4.00	3+	E-5-D.9	1	1902	1	4.00	46	1.19	1.38	1.00	302	254	7.50	8.0	0.75	0.38	8.00	0.00	5.0	5.0	5.00	2.50	5.00	1.00	1.00	0.00	0.96	0.61	1.00	1.62	1.50	4.00	0.99	1.63	3.0	4.0



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Specimen ID and Location						Section 4.1.0 Geometry Calculations - Uniform Force Method																							Section 4.2.0 Gusset Stress Calculations																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																	
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											L _{cb}	L _{1cb}	L _{bb}	L _{1bb}	L _{tb}	L _g	e _{Col}	e _{Bm}	I _{gc,min}	I _{gb,min}	α min	WD _{Bm,in}	WD _{Bm,Out}	α _g	α _{bar}	β min	WD _{Col,in}	WD _{Col,Out}	β _g	β _{bar}	K	K'	D	a _{nE}	β _{nE}	r	φ _w	n _i	n _o	s	F _{Yg}	F _{Ug}	t _g	t _{r,Des}	Whmt Ang	L _{Br}	Y1	X2	h _{Br}	Full Ht	h _{Bm}	h _{Col}	Constrain	A _{wh}	Φ _{Rn-w}	E _{st}																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																						
EOR-ID	Line	Grids	Lvls	Mark	Qty	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in	in</

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Specimen ID and Location						4.2.2 Gusset Plate Buckling										Section 4.2.3 Gusset Plate Buckling (Out-of-Plane)																				
																A. Consider Self Weight of Brace Out-of-Plane Acting on Gusset					B. Consider Adjusted Brace Strength Out Of Plane Frame Deformation															C. Consider Total Moment from Part A and B
EOR-ID	Line	Grids	Lvls	Mark	Qty	ϕ_{gb}	E_{Gst}	K_{gb}	L'	r_g	λ	ϕR_{n-gb}	P_{uc}	S_A	Factor	I_p	W_{tBRB}	$F_{Add'l-OOP/End}$	$SW F_{OOP}$	$M_{Arm-OOP}$	$SW M_{OOP}$	Factor	SD	Drift Angle	Factor	P_H	M_{Arm-PH}	M_{PH}	M_u	L_c	L_b	L_t	Z_g	ϕMn	$\frac{M_u}{\phi Mn}$	DCR
#		#	#	#	#		ksi	in	in	in		kip	ϕR_{n-gb}	(SDS)	on S_A		kips	kips	kips	in	k-in	on SD	%	RAD	on ABS	kips	in	k-in	k-in	in	in	in	in ³	k-in	ϕMn	$_{gb+fl}$
BRB-4.00	3+	E-5-D.9	2	1901	1	0.90	29000	1.00	3.31	0.29	0.15	601	0.51	1.00	0.40	1.00	0.86	0.00	0.17	21.25	3.68	0.67	1.00%	0.01	100%	2.046	5.625	11.509	15.2	13.0	12.3	25.3	6.32	284	0.05	0.56
BRB-4.00	3+	E-5-D.9	1	1902	1	0.90	29000	1.00	4.91	0.29	0.23	594	0.51	1.00	0.40	1.00	0.88	0.00	0.18	21.25	3.74	0.67	1.00%	0.01	100%	2.014	5.625	11.331	15.1	14.9	13.8	28.8	7.19	324	0.05	0.55



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#		#	#	#	#	in ²	ksi				kip	kip	in	in	in	in	in	in	in	in	in	in	in		in	rad	rad	in	in	in	in	in	in	in	in	
BRB-4.00	3+	E.5-D.9	2	1901	1	4.00	46	1.20	1.39	1.00	307	256	7.50	8.0	0.38	-	0.00	8.0	8.0	0.75	0.38	-	1.00	1.00	0.00	0.95	0.63	1.00	1.09	1.00	0.90	0.99	1.625	3.0	4.0	4.0
BRB-4.00	3+	E.5-D.9	1	1902	1	4.00	46	1.19	1.38	1.00	302	254	7.50	8.0	0.38	-	0.00	8.0	8.0	0.75	0.38	-	1.00	1.00	0.00	0.96	0.61	1.00	1.01	1.00	0.35	0.99	1.625	3.0	4.0	4.0



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Specimen ID and Location						Section 4.1.0 Geometry Calculations - Uniform Force Method																						Section 4.2.0 Gusset Stress Calculations																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																	
						Length from WP to Tip of BRB						Length from Square Projection to Edge of Gusset (CB Lap on Gusset)																		4.2.1 Whitmore Section Stress Check																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																															
EOR-ID	Line	Grids	Lvls	Mark	Qty	L _{ct}	L _{1ct}	L _{bt}	L _{1bt}	L _{tt}	L _t	L _g	e _{Col}	e _{Bm}	I _{gc,min}	I _{gb,min}	I _{gc,ext}	I _{gb,ext}	α min	WD _{Bm,in}	WD _{Bm,Out}	α _g	α _{bar}	β min	WD _{Col,in}	WD _{Col,Out}	β _g	β _{bar}	K	K'	D	α	β	r	φ _w	n _i	n _o	n _b	s	F _{yg}	F _{ug}	t _g	t _{r,Des}	Whtm Ang	L _{Br}	Y1	X2	h _{Br}	Full Ht	h _{Bm}	h _{Col}	Constrain	A _{wh}	W _{wh}	A' _{wh}	Φ _{Rn-W}	P _u																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																				
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BEAM/COL FLANGE TOP CONNECTION

Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

Specimen ID and Location						4.2.2 Gusset Plate Buckling						Section 4.2.3 Gusset Plate Buckling (Out-of-Plane)																									
												A. Consider Self Weight of Brace Out-of-Plane Acting on Gusset								B. Consider Adjusted Brace Strength at Out-of-Plane Frame Deformation						C. Consider Total Moment from Part A and B											
EOR-ID	Line	Grids	Lvls	Mark	Qty	ϕ_{gb}	E_{gst} ksi	K_{gb}	L' in	r_g in	λ_c	ΦR_{n-gb} kip	P_{unc} ΦR_{n-gb}	S_A (SDS)	Factor on S_A	I_p	W_{tBRB} kips	$F_{addtl-OOP/End}$ kip	$SW F_{OOP}$ (EA End) kips	$M_{Aim-OOP}$ in	$SW M_{OOP}$ k-in	Factor on SD	SD %	Drift Angle RAD	Factor on ABS	P_H kips	M_{Aim-PH} in	M_{PH} k-in	M_u k-in	L_c in	L_b in	L_t in	Z_g in³	ϕMn k-in	$\underline{Mu}$ ϕMn	DCR g_b+t	
#		#	#	#	#	ϕ_{gb}	ksi		in	in		kip	ΦR_{n-gb}	(SDS)			kips	kip	kips					%			kips	in	k-in	k-in	in	in	in	in³	k-in	ϕMn	
BRB-4.00	3+	E.5-D.9	2	1901	1	0.90	29000	1.00	3.18	0.29	0.15	602	0.51	1.00	0.40	1.00	0.86	0.00	0.17	21.25	3.68	0.67	1.00%	0.01	100%	2.05	5.63	11.51	15.18	12.26	13.04	25.30	6.32	284.61	0.05	0.56	
BRB-4.00	3+	E.5-D.9	1	1902	1	0.90	29000	1.00	3.24	0.29	0.15	601	0.50	1.00	0.40	1.00	0.88	0.00	0.18	21.25	3.74	0.67	1.00%	0.01	100%	2.01	5.63	11.33	15.07	12.27	12.77	25.04	6.26	281.75	0.05	0.55	

Reed College Central Plant Upgrade

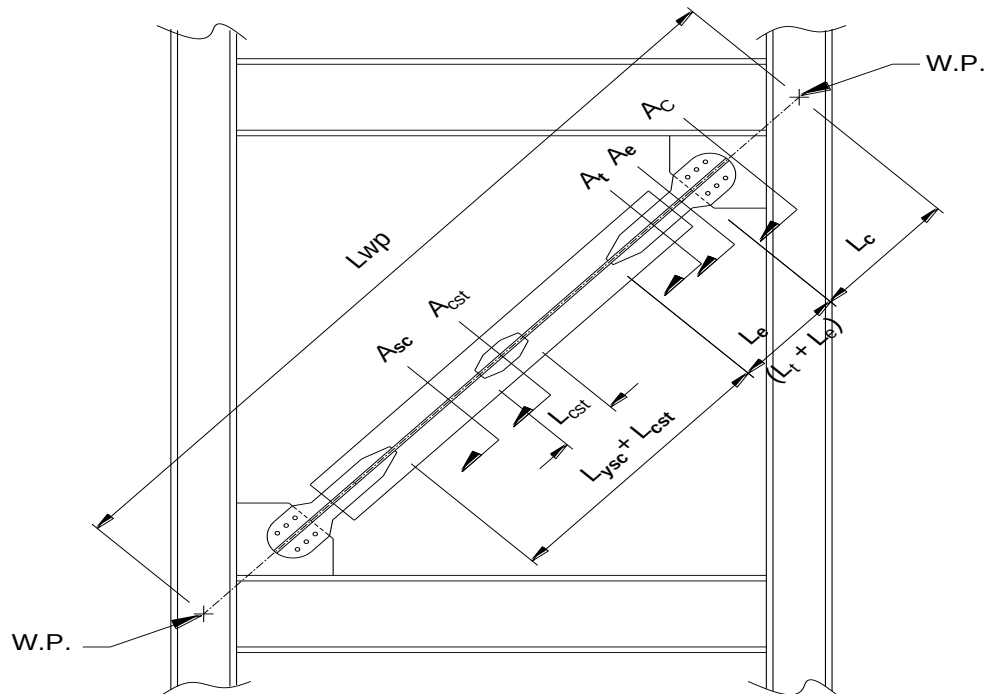
Calculation Submittal Package

Description

Section 7. Stiffness Sample Calculation
 Stiffness Tables

Stiffness Calculation

Example Mark #: 1901
Line 3+, Grid E.5-D.9, Level 2



Stiffness Calculation**7.0 DESIGN CRITERIA**

Length Between Work Points at Top and Bottom of Brace	L_{WP} :	150.4 in	(3819 mm)
Modulus of Elasticity	E:	29000 ksi	(199955 MPa)
Yielding Core Stiffness			
Yielding Core Length	L'_{YSC} :	69.3 in	(1760 mm)
Yielding Core Area	A_{YSC} :	4.00 in ²	(2581 mm ²)
Yielding Core Stiffness $K_{YSC} = A_{YSC} \cdot E / L_{YSC}$	K_{YSC} :	1674 k/in	(293 kN/mm)
End Zone Stiffness			
Length of Stiffener Plate Extension into Casing	L_e :	16.7 in	(425 mm)
End Zone Total Length $L_{ET} = 2L_e$	L_{ET} :	33.5 in	(850 mm)
End Zone Area	A_e :	8.98 in ²	(5792 mm ²)
End Zone Stiffness $K_e = A_e \cdot E / L_{ET}$	K_e :	7782 k/in	(1363 kN/mm)
Transition Zone Stiffness (Where Occurs)			
Length from End of Stiffener Plate to Middle of Final Transition	L_t :	0.0 in	(0 mm)
Transition Zone Total Length $L_{tT} = 2L_t$	L_{tT} :	0.0 in	(0 mm)
Transition Zone Area	A_t :	0.00 in ²	(0 mm ²)
Transition Zone Stiffness $K_t = A_t \cdot E / L_{tT}$	K_t :	--	--
Connection Stiffness			
Length of Connection from Work Point to End of Gusset	L_c :	23.8 in	(605 mm)
Connection Region Total Length $L_{cT} = 2 \cdot L_c$	L_{cT} :	47.6 in	(1210 mm)
Connection Area	A_c :	26.93 in ²	(17376 mm ²)
Connection Stiffness $K_c = A_c \cdot E / L_{cT}$	K_c :	16401 k/in	(2872 kN/mm)
Center Region Stiffness (Not Applicable Where $L_{cst} = 0$)			
Length of Center Region	L_{cst} :	0.0 in	(0 mm)
Area of Center Region	A_{cst} :	4.00 in ²	(2581 mm ²)
Center Stiffness $K_{cst} = A_{cst} \cdot E / L_{cst}$	K_{cst} :	--	--
Total Stiffness $K_{eff} = 1 / (1/K_{YSC} + 1/K_e + 1/K_t + 1/K_c + 1/K_{cst})$	K_{eff} :	1271 k/in	(223 kN/mm)
Yielding Core Stiffness WP to WP $K_{LWP} = A_{YSC} \cdot E / L_{WP}$	K_{LWP} :	771 k/in	(135 kN/mm)
Stiffness Modification Factor $K_f = K_{eff} / K_{LWP}$	K_f :	1.65	

Length Verification

$$\frac{L_{YSC} + L_{eT} + L_{tT} + L_{cT} + L_{cst}}{L_{WP}} = 1.00 \quad \text{Should be 1.0 if all regions are accounted for.}$$



COREBRACE STIFFNESS CALCULATIONS

Project: Reed College Central Plant Upgrade
Location: Portland, OR
Job: 6903

Specimen ID and Location						General		Yielding Core Stiffness			End Zone Stiffness				Transition Zone Stiffness				Connection Stiffness				Center Region Stiffness			Total Stiffness & Check			
EOR-ID #	Line	Grids #	Lvls #	Mark #	Qty #	L _{wp} in	E ksi	L _y sc in	A _{sc} in ²	K _y sc k/in	L _e in	L _e T in	A _e in ²	K _e k/in	L _t in	L _t T in	A _t in ²	K _t k/in	L _c in	L _c T in	A _c in ²	K _c k/in	L _{cst} in	A _{cst} in ²	K _{cst} k/in	K _{Eff} k/in	K _{LWP} k/in	K _F	Length Check
BRB-4.00	3+	E.5-D.9	2	1901	1	150	29000	69.3	4.00	1674	16.7	33.5	9.0	7782	0.0	0.0	0.00	-	23.8	48	26.9	16401	0.0	4.0	-	1271	771	1.65	1.0
BRB-4.00	3+	E.5-D.9	1	1902	1	154	29000	71.5	4.00	1623	16.6	33.3	8.9	7743	0.0	0.0	0.00	-	24.5	49	26.6	15787	0.0	4.0	-	1236	755	1.64	1.0